Design of Optimal LLCL Filter with an Improved Control Strategy for Single Phase Grid Connected PV Inverter

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ABSTRACT

The third order LLCL filter is gaining more attractive in grid connected PV inverter in terms of material cost saving than LCL filter. Several active and passive damping techniques prevail in mitigating the resonance problem for maintaining the grid power quality standards. In this paper an improved passive damping is examined with reduction of power loss for the LLCL filter. Particularly, it reduces the switching ripple much better than LCL filter, with a decrease in volume of the inductance. The filter design is also developed for the operation of stiff grid. Mathematical operations and transfer function are derived with frequency response for the accuracy of the filter design. In addition, comparative analysis of passive and improved passive damping control is proposed. The control strategy is improved with feedback linearization in order to avoid the glitches in inverter control and is verified with prototype grid connected PV inverter.

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1. INTRODUCTION

With the increase in distributed power generation systems (DPGs) it has become mandatory to supply excess power to the existing grid with the standard grid codes [1]. Figure 1. shows the generic structure of single phase grid connected PV inverter with controlled LCL filter design. The interconnection between DC converter and inverter is operated by dc-link capacitor.

Figure 1. Control structure of single phase grid connected PV inverter
The power from the photovoltaic (PV) is injected into the grid through the voltage source inverter (VSI). Among many topologies [2]-[4], transformerless inverters have attracted due to its physical size with less space requirements and feasible cost constraints. The pulse width modulation (PWM) control is achieved by closed loop current control with the current harmonics less than 5% [5]. The switching frequencies between 2-15 kHz causes higher order harmonic disturbances in grid and losses. Higher order harmonics into the grid due to switching frequencies, leakage current and the electromagnetic interference (EMI) [6] noise are the significant issues in designing of filter circuit in the PV inverter.

Ripples and harmonics in the grid current can be reduced by filters connected at the output of the inverter [7]. The first order filter consists of one inductor connected in series known as L-filter which is most commonly used [8]. It does not have a resonance problem as compared to higher order filters. The inductor achieves reasonable attenuation of the current harmonics. The attenuation of 20 dB/decade is achieved for high frequency PWM converters. Higher order filters, LC & LCL have the combinations of inductors and capacitors, can give better attenuation of the harmonics with the disadvantages of complex design, cost and bulky [9]. The LC filter has better damping characteristics, but suffers from problem of infinite gain at resonance. In grid connected system, the resonance frequency of the filter varies with the inductance value of the grid [10]. The control of LCL filter is difficult compared to L filter, due to the presence of two more poles and zeros. Care must be taken to design a controller for additional poles and zeros that can make the system unstable if proper damping is not introduced. Damping of the LCL filter resonance can be either active using the converter, or passive using elements like resistors, capacitors and inductors. Several methods of passive damping [11]-[12] have been proposed for stiff grid operation. On the other hand, the active damping method is used with costly sensors and power electronics for weak grid and dynamic grid variations.

This paper mainly focuses on control structure of single phase grid connected PV inverter with filter design analysis. Section II illustrates the constraints of the LCL filter design and importance of Q-factor with sensitivity analysis. An improved LLC filter is introduced, in order to reduce the total inductance of the conventional filter. The modified LLC filter is designed without any change in the frequency response characteristic of LCL filter. More advantage in suppressing the resonance peak with improved stability and dynamic response. Three cases of parameter design have been differentiated and analyzed with simulated results in section III. Improved current control structure is seen in section IV by implementing feedback linearization for fast DC voltage control applied to PWM inverter. And it is verified by modeling a single phase grid connected PV inverter with simulated and experimental results.

2. SYSTEM DESCRIPTION AND CHARACTERISTICS
2.1. Classical Methods and Constraints on LCL Filter Design
In grid power converters, switching frequencies at intervals 3–20 kHz causes greater harmonics and disturbs the electric grid. It is therefore essential to attenuate the switching frequency harmonics and reduce the current ripples to fulfill the standards of the IEEE 1547.2. High frequency component currents would lead to electromagnetic interference noise mainly due to the parasitic capacitance disturbing the behavior of high frequencies. The method of designing LCL filters depends on rating of power converters, fundamental and switching frequency as inputs with an integrated control design of filters as explained in [13]. From the Figure 2 (a), the inverter output inductor L1, the filter capacitor C1, and the grid-side inductor L2 constitute the LCL filter of the inverter. Compared to L filter, LCL filter is proved to have a better harmonic attenuation for the reduction of filter inductance volume [14] which bypass the high frequency harmonics through the capacitance branch. The scope is to lower the higher order harmonics on the grid side and to reduce the oscillation effects. Therefore, in LCL filter design, inductors should be properly designed in observing the current ripple, filter capacitance and damping of resonance in filters. The resonant frequency should be in the range 10ω0 ≤ ωres ≤ ωsw/2 [15]. Figure 2 (b), (c) depicts the passive damped topology of LCL filter. Frequency response analysis of passive damped LCL filters with damping resistors in series to attenuate the resonance with the transfer function as in (1) and improved methods with passive elements as in (2) are shown in Figure 3.
Figure 2. a). LCL filter, b) passive damped LCL filter with $R_d$, c) passive damped LCL filter with $R_d$-$C_d$

Transfer function of LCL filter:

$$G_{v_i \rightarrow i_g}(s) = \frac{i_g(s)}{v_i(s)} = \frac{1}{L_2} \left( \frac{S^2 + Z_{LC}^2}{S^2 + \omega_{res}^2 + \omega_{res}^2} \right)$$

(1)

If $R_d$ is zero then,

$$G_{v_i \rightarrow i_g}(s) = \frac{i_g(s)}{v_i(s)} = \frac{1}{L_2} \left( \frac{S^2 + Z_{LC}^2}{S^2 + \omega_{res}^2} \right)$$

Where,

$$Z_{LC}^2 = [L_1 C_f]^{-1}$$

$$\omega_{res}^2 = \frac{Z_{LC}^2 L}{R_d}$$

For improved passive damping,

$$G_{v_i \rightarrow i_g}(s) = \frac{i_g(s)}{v_i(s)} = \frac{(R_d C_d S + 1)}{S(L_1 L_2 R_d C_d C f S^2 + L_1 L_2 C_d C f S^2 + R_d C_d (L_1 + L_2) S + L_1 L_2)}$$

(2)

From Figure 3 it is clear that the magnitude of LCL filter is high with a resonant peak gain of 250 dB at 4.6 kHz. However, in passive damping and improved passive damping, the attenuation is reduced to 10 dB or less than that at 2.5 kHz with some power loss due to the resistor.

Figure 3. Frequency response of LCL filter
2.2. Selection of Filter Capacitance (Cf)

The selection of capacitor [16] is determined between reactive power in Cf and L1. If the capacitance is high, the reactive power flowing into it is more which leads to current demands in L1. In the design consideration large inductance (L1) and smaller capacitance (Cf) lead to the voltage drop across the inductor L1. So, reactive power is chosen 15% of rated power as in (3) and from that the capacitance value can be chosen as:

\[ C = 15\% \frac{P_{rated}}{3 \times 2\pi f_{line} V_{rated}^2} \]  

(3)

Where, \( P_{rated} \) is rated power and \( V_{rated} \) is grid RMS voltage.

2.3. Significance of Q-factor Analysis

The importance of damping is to lower the Q-factor at the resonant frequency without affecting the frequency response at other frequencies. In Figure 3 frequency response analysis of higher order filter with and without damping is analyzed. The series LC circuit gives a minimum impedance at resonance while parallel LC circuit gives a maximum impedance at the resonant frequency. The value of Q-factor reduces in passive damping at a dominant resonant frequency [17]. The quality factor of \( L_{c}C_f \) can be expressed as,

\[ Q = \frac{1}{R_f} \sqrt{\frac{L_f}{C_f}} \]  

(4)

For reducing the peak resonant, damping resistor is designed with an optimal Q-factor for the stiff grid condition. Increase of grid inductance can reduce the passive damping effect and cannot achieve the optimal Q-factor. Concurrently, the total power dissipation in the damping circuit is also an important parameter.

3. DESIGN OF MODIFIED LLCL FILTER

Based on the traditional LCL filter, a small inductor is inserted in the branch loop of the capacitor, composing a series resonant circuit at the switching frequency. It can, particularly, attenuate the switching-frequency current ripple components much better than the LCL filter, saves the total inductance and thereby leads to size reduction. The most convenient passive method is by adding physical resistors connected either in series or in parallel with inductor or capacitor of the filter. It aims at reducing Q-factor at dominant resonant frequency. Recently to reduce the inductor size a novel higher order LLCL filter [18] is proposed as shown in Figure 4 with transfer function as in (5)

![Figure 4. Schematic diagram of LLCL filter](image_url)

Transfer function of \( \frac{i_g(s)}{v_i(s)} \) LLCL filter is given as

\[ G_{v_i \rightarrow i_g}(s) = \frac{i_g(s)}{v_i(s)} = \frac{L_f C_f s^2 + 1}{(L_1 L_2 L_f + (L_1 + L_2)) L_f C_f s^3 + (L_1 + L_2)L_f C_f s^2} \]  

(5)

For LLCL, \( \omega_{res} = \frac{1}{\sqrt{(L_1 L_2 L_f + L_f) C_f}} \)
3.1. Passive Damped Scheme of LLCL Filter

Modified LLCL filter topology [19] is used to reduce the damping power loss and high frequency harmonic attenuation as shown in Figure 5 (a), (b). Because of a series resonant circuit $L_fC_f$ is at switching frequency, the value of the inductor is much smaller than that of $L_1$ & $L_2$. From the Figure 5 (b) passive damped LLCL & Figure 2 (c) improved passive damped LCL, the value of damping parameters $R_d$ and $C_d$ is same. Most significantly, the total capacitance of ($C_d+C_f$) is encouraged to be less than 5% of apparent reactive power at rated load. From (6) and (7) it is to be noted that the addition of poles and zeros in a system gives rise to stability issues and care should be taken in designing the filters.

![Figure 5. Various passive damped LLCL filters with $R_d$ and $C_d$. a) LLCL, b) LLCL.](image)

Bode plot of the transfer function of (1) & (5) is depicted as in Figure 6 a) and it is clear that an LLCL filter based grid connected VSI has almost same frequency response characteristic of LCL filter. In Figure 6 b) the peak magnitude lies within 20 kHz, the first resonant peak occurs at 7.6 kHz within half of the switching frequency and the next peak occurs at 20 kHz. The damping technique minimizes the resonant peak within the range. And it is worth mentioned that compared to LCL filter, the additional inductor $L_f$ does not bring any control difficulties, an additional grid inductance $L_2$ is added to widen the bandwidth.

Transfer function of improved passive damping LLCL1

$$G_{r_i \rightarrow i_g} (s) = \frac{i_g(s)}{v_i(s)} = \frac{s^3A+s^2B+sC+1}{s^5A+s^4B+s^3C+s^2D+se}$$

(6)

$$a=L_1L_2L_fC_fC_d$$
$$b=((L_1L_2+(L_1+L_2)L_f)R_dC_fC_d)$$
$$c=((L_1L_2(C_d+C_f)+L_fC_f(L_1+L_2))$$
$$d=R_dC_d(L_1+L_2)$$
$$e=(L_1+L_2)$$
$$A=L_1C_fC_dR_d$$
$$B=L_2C_f$$
$$C=R_dC_d$$

Transfer function of improved passive damping LLCL2:

$$G_{v_i \rightarrow i_g} (s) = \frac{i_g(s)}{v_i(s)} = \frac{s^3A'+s^2B'+sC'+1}{s^5A'+s^4B'+s^3C'+s^2D'+se'}$$

(7)

$$b'=((L_1L_2+(L_1+L_2)L_f)R_dC_fC_d)$$
$$c'=((L_1L_2(C_d+C_f)+L_f(C_d+C_f)(L_1+L_2))$$
$$d'=R_dC_d(L_1+L_2)$$
$$e'=(L_1+L_2)$$
$$A'=L_1C_fC_dR_d$$
$$B'=L_2C_f$$
$$C'=R_dC_d$$

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Table 1. Filter Parameters in Design

<table>
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<th>Case-II</th>
<th>Case-III</th>
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<tbody>
<tr>
<td>L1</td>
<td>1.2mH</td>
<td>1.2mH</td>
<td>1.2mH</td>
</tr>
<tr>
<td>R1</td>
<td>0.1Ω</td>
<td>0.1Ω</td>
<td>0.1Ω</td>
</tr>
<tr>
<td>L2</td>
<td>1.2mH</td>
<td>1.2mH</td>
<td>0.22mH</td>
</tr>
<tr>
<td>R2</td>
<td>0.04Ω</td>
<td>0.04Ω</td>
<td>0.01Ω</td>
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<tr>
<td>Lf</td>
<td>-</td>
<td>-</td>
<td>32μH</td>
</tr>
<tr>
<td>Rf</td>
<td>-</td>
<td>-</td>
<td>0.2 Ω</td>
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<tr>
<td>Cf</td>
<td>-</td>
<td>2μF</td>
<td>2μF</td>
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<tr>
<td>Rd</td>
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<td>30Ω</td>
<td>16.5Ω</td>
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<tr>
<td>Cd</td>
<td>4μF</td>
<td>2μF</td>
<td>2μF</td>
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4. SYSTEM MODELING AND CONTROL STRUCTURE

The bode plot of LCL and LLCL filter parameters, as given in Table 1 is plotted in Figure 7 with the sensitivity analysis on parameter variation of ±20%. The enlarge view of magnitude of LLCL filter is also shown. Moreover, case I & case III as in Table 1 attenuate the resonance by -40 dB/decade, but in case II it is -60 dB/decade as in Figure 8. The designed LLCL filter attenuates resonant harmonics around the switching frequency and well suited for the single phase system.
4.1. Proposed Inverter Current Control Strategy

The current injected into the grid by a power converter should keep a certain relationship with voltage at a point of connection. In order to avoid the glitches in the control of inverter it should be made more robust with the accurate parameter analysis. The block diagram in Figure 9 shows conventional current control loop structure [19] with grid side current feedback control. Where, $G_p(s)$ expressed as process gain & $G_C(s)$ denotes proportional resonant (PR) and harmonic compensator (HC) controller gain, $H(s)$ implies feedback gain of grid injected current, $G_{inv}(s)$ indicates gain of inverter and $G_{vg \rightarrow Ig}(s)$ denotes a transfer function of LLCL filter, given by (5).

![Figure 9. Inverter power control loop](image)

![Figure 10. Proposed inverter current control structure](image)

<table>
<thead>
<tr>
<th>Parameters</th>
<th>CASE I</th>
<th>CASE II</th>
<th>CASE III</th>
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<tr>
<td>THD</td>
<td>2.48 %</td>
<td>3.5 %</td>
<td>2.4 %</td>
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<tr>
<td>Simulation</td>
<td>3.82 %</td>
<td>4.04 %</td>
<td>3.5 %</td>
</tr>
<tr>
<td>Experimental</td>
<td>2.51</td>
<td>0.89</td>
<td>0.45</td>
</tr>
<tr>
<td>Calculated</td>
<td>2.57</td>
<td>0.91</td>
<td>0.52</td>
</tr>
<tr>
<td>Measured</td>
<td>2.57</td>
<td>0.91</td>
<td>0.52</td>
</tr>
</tbody>
</table>

By considering the LLCL filter as shown in Figure 4i, the inverter current and the current flows through the capacitor $i_c$ is being negligible compared to $i_1$. The inverter current control structure as in Figure 10 exhibits the calculation of inverter current $i_1$ from the duty ratio (D) needs grid voltage ($V_g$) that is related to $i_1$ by the undetermined grid impedance ($Z_{grid}$). To avoid this problem, a nonlinear control technique from modern control theory named feedback linearization scheme [20], [21] is proposed. To exhibit the undetermined grid impedance, $V_g$ is treated as a DC parameter. Compared to inverter current $i_1$ that is, the current loop crossover frequency is much higher than grid frequency. The Figure 10 also shows duty cycle (D) calculation from $V_i$ using $V_g$ and $V_{DC}$ as defined in (8). With the proposed control the respective parameter makes the linear system with reduction in capacitor ripple current [22] and therefore reducing the size of the capacitor. The instantaneous current reference is used by the current compensator with the feedback current to provide a duty ratio to the inverter. The DC bus voltage is fixed at the desired set point and controlled current is injected into the grid. Here $V_i$ controls the main inductor current $I_L$. The inverter current fed into the grid is given by (9). Where $K_s$ represents the current feedback gain. Hence, the loop gain transfer function is expressed as,
\[ G_{\text{loop}}(s) = G_c(s)K_sG_p \]

For the synchronization purpose, second order generalised integrator phase locked loop (SOGI-PLL) technique [23,24] is used to synchronize inverter voltage to the grid voltage and frequency.

\[ D = \frac{(i_g - i_d)G_c(s) + V_g}{v_{DC}} \quad (8) \]

\[ i_p = \frac{(v_{DC} + D) - V_g}{Z_{\text{LCL}}} \quad (9) \]

4.2. Experimental and Simulation Results

In order to verify the proposed damping technique and control structure, simulation is carried out using MATLAB/Simulink software. The parameters are the same as the designed in Table I. In order to verify the theoretical analysis, a 250 W experimental prototype as in Figure 11 based on a DSP (TMS320F28035) controller is constructed. A programmable DC power supply (chroma 62012P-80-60) is used to emulate the renewable energy sources. The grid current is sensed by current sensor ACS712ELCTR-20A, the type of IGBTs is IRFB4227PBF with switching frequency (F_s) as 20 kHz. A DC link capacitor of united chemi-con KXG series 450 V, 100 μF is used. Total harmonic distortion (THD) is measured by the Fluke-434-Power quality analyzer and the waveform is obtained with agilent (MSO). Grid voltage and frequency are normally 230 V/50 Hz.

With the feedback linearization control, Figure 12 shows the steady state experimental voltage response of dc-link voltage of 388 V as input to the inverter. The grid voltage and inverter output voltage synchronization in Figure 13 a) shows this as a promising current control structure with grid voltage and inverter voltage synchronized each other. The waveforms of inverter output voltage before filtering is shown in Figure 13 b). With the conventional LCL filter parameters the waveform of voltage and current is shown in Figure 14 with harmonics and spikes. To validate the proposed control structure and filter design, experimental results of both LCL and LLCL filter output waveform is compared in Figure 15 a), b). It shows that the proposed design of LLCL filter has less distortion in the waveform compared to LCL filter as the THD is 3.5 % with the proposed LLCL filter and 3.82 % with the conventional LCL filter as mentioned in Table 2. The results of the proposed grid connected system is shown in experimental results as in Figure 16 peak to peak voltage of 164.3 V and grid injected current of 2.2 A. The total harmonic distortion of the grid current in the laboratory is THD=3.5% as shown in Figure 17 that meets the IEEE 519 standard by measuring with the power quality analyzer FLUKE-434.

4.3. Result Analysis and Discussion

From the results it is to be that, increasing grid inductance can reduce the passive damping effect and increases the losses in the circuit in case I & II in Table I. However, in case III resonant peak occurs within the switching frequency with limited magnitude attenuation and current harmonic around it satisfy IEEE 519-1992. The current harmonic (>=35th) is less than 0.3% of fundamental current by the parameter drift of L_2 in range ±20% both in switching frequency and double of switching frequency. The proposed improved control strategy enhances the performances by introducing feedback linearization making linear structure in adding integrators to get fast and zero tracking errors and reducing the capacitor value as 100 μF.

The total harmonic distortions of the grid side current in the three cases are measured using simulation and experiments and are listed in Table II. In case III, LLCL filter (L_1=1.2 mH, L_2=0.22 mH, L_{pf}=0.032 mH) are used, of which the control performance of the grid inverter is shown in Figure 17 and THD is calculated as 2.4% in simulation and 3.5% in experimental. The damping loss calculation as in [8]. The power losses in the filter are mainly caused by inverter-side inductor current ripples of both LCL and LLCL filter. The damping power loss is mainly caused by volume of L_2, L_4 and R_d with the calculated and measured value of LLCL filter as 0.45 W and 0.52 W less than LCL filter.
Figure 11. Laboratory setup of grid connected PV system

Figure 12. Experimental steady state DC bus voltage

Figure 13. (a) Synchronization of inverter voltage and grid voltage (b) Simulated inverter output voltage

Figure 14. Experimental waveform of voltage and injected current into grid: a) with LCL filter
5. CONCLUSIONS

For reducing the resonance in the filter circuit, damping resistors are added with an additional inductance in LCL filter with improved control strategy is proposed in this paper. Comparative damping analysis of LCL and LLCL filter is designed with case parameters defined. Addition of passive elements and variation in filter parameters does not lose the stability. A Feedback linearization is used to control the duty ratio of inverter control for fast dynamic process, by adding integral control to eliminate steady state error that enhances the performance and shows satisfactory behaviour. The voltage transient is improved to decrease of current ripple and the size of the capacitor is reduced. The robustness of the system are verified using simulated and experimental results. The waveform of output current without any distortion shows that
the inverter with proposed control structure can convert solar power to a high quality power into the utility grid.

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NOMENCLATURE

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<th>Symbol</th>
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<tr>
<td>V_i</td>
<td>inverter voltage (V)</td>
</tr>
<tr>
<td>V_g</td>
<td>grid voltage (V)</td>
</tr>
<tr>
<td>P_{rated}</td>
<td>rated power (W)</td>
</tr>
<tr>
<td>F_{grid}</td>
<td>grid frequency (Hz)</td>
</tr>
<tr>
<td>C_f</td>
<td>filter capacitance</td>
</tr>
<tr>
<td>R_d</td>
<td>damping resistor</td>
</tr>
<tr>
<td>C_d</td>
<td>damping capacitance</td>
</tr>
<tr>
<td>\omega_0</td>
<td>fundamental frequency</td>
</tr>
<tr>
<td>D</td>
<td>duty ratio</td>
</tr>
<tr>
<td>i_1</td>
<td>inverter current (A)</td>
</tr>
<tr>
<td>i_g</td>
<td>grid current (A)</td>
</tr>
<tr>
<td>V_{rated}</td>
<td>rated voltage (V)</td>
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<tr>
<td>V_{DC}</td>
<td>dc bus voltage (V)</td>
</tr>
<tr>
<td>Z_{grid}</td>
<td>grid impedance</td>
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</table>

REFERENCES


**BIOGRAPHIES OF AUTHORS**

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