DC traction power substation using eighteen-pulse rectifier transformer system

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ABSTRACT

Twelve-pulse rectification system had been widely integrated in today’s DC traction power sub-station (DC-TPSS). This configuration had successfully mitigated low order harmonic distortion. As some research findings had confirmed that the DC voltage and current ripple factors may further be minimized by increasing the number of rectification pulses to 18, 24, or 36. This paper had presented a simulation study to investigate the prospect of implementing an eighteen-pulse rectification system in a DC-TPSS. The theory of phase-shifting transformer used to produce an 18-pulse rectifier is presented with simulation verification. Simulation result shows that 3.69% of grid current distortion index is recorded without installing any filters. In addition, the DC voltage and current ripple may also be further reduced for about 30% compared to a conventional twelve-pulse rectification system.

Keywords:
DC traction power substation
Harmonic mitigation
Multipulse rectifier
Phase-shifting transformer
Total harmonic distortion

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1. INTRODUCTION

Most of the urban metros are powered by standard DC railways voltages rated at 750 V. A typical DC traction power substation is generally consists of a traction transformer and rectifier [1], [2]. The conventional six-pulse rectifier has first been integrated [3] in the substation. Unfortunately, significant harmonics distortion is observed both in ac and DC terminals. As a result, to meet the harmonics requirements [4], bulky and costly passive filters are being installed [5], [6].

With the invention of phase-shifting transformer [7], multipulse rectifier transformer system has started to be used in DC traction power substation. Figure 1 illustrates a twelve-pulse rectifier transformer system which is employed in a DC traction power substation. The main advantage offers by this system is that the low order ac harmonics will be cancelled out automatically. This is mainly cause by the phase angle displacement produced by the phase-shifting transformer. In addition, the DC voltage and current ripples will also be reduced. As a result, the size of passive filters had been reduced drastically. It is highlighted that by increasing the number of pulses in rectification, the quality of voltage and current waveforms will be further improved [8], [9].

Many research findings have denoted that an eighteen-pulse rectifier transformer system may help to further reduce total harmonics distortion (THD) ranging from 2%-3% compare to a commonly used 12-pulse system [10]-[12]. Therefore, this paper will present a simulation study of integrating an eighteen-pulse rectifier transformer system in Malaysia light-rail-transit (LRT) traction power substation. The main...
objective is to estimate the power quality improvement on ac lines and the ripple factor reduction on DC terminal compared to the existing 12-pulse rectification system. The paper is outlined with presenting the theories of 12-pulse and 18-pulse rectifier transformer systems in Section 2. Section 3 presents simulation analysis for both systems and a conclusion will be summarized in Section 4.

Figure 1. DC Railway Traction Power Substation employing a 12-pulse rectifier transformer system [13]

2. MULTI-PULSE RECTIFIER TRANSFORMER SYSTEM

Multipulse rectifier transformer systems have been proposed to enhance the conventional rectification system in various applications. For instance, variable frequency drives [14]-[16], HVDC [17], renewable energy power transmission [18], [19], and aircraft based power supply system [20], [21]. Phase-shifting transformer is the most essential components used to realize 12-pulse, 18-pulse, 24-pulse, or even higher pulses of rectification. Unfortunately, the project cost and circuit complexity will also increase proportionally to the number of pulses [22], [23]. Hence, an 18-pulse rectifier transformer system is investigated for future Malaysia’s LRT power substation.

2.1. Twelve-pulse rectifier transformer system

The existing 12-pulse rectifier transformer system configured in the traction power substation is presented in Figure 2 (a) [24]. A balance three phase utility supply, \( v_g \), is assumed to power up the power substation. The three phase voltages can be expressed as:

\[
\begin{align*}
    v_A &= V_m \sin (\omega t) \\
    v_B &= V_m \sin (\omega t - 120^\circ) \\
    v_C &= V_m \sin (\omega t + 120^\circ)
\end{align*}
\]  

(1)

Where \( V_m \) is the peak voltage value of the phase voltages and \( \omega \) represents the angular frequency of the grid.

A three windings phase-shifting transformer is integrated in between the utility grid and two units of 6-pulse diode rectifiers. These identical rectifiers are connected in parallel. The rectifier power circuit is shown in Figure 2 (b). The delta-connected primary winding of the transformer is configured with \( N_1 \) turns. In order to produce a 30\(^\circ\) phase shifting at its secondary output terminals, two set of coils with \( N_2 \) and \( N_3 \) turns are configured in delta and star connection as shown in Figures 2 (c) and (d). The turn ratio of the transformer can be determined from the effective voltage drop acrossed the coils.

\[
\begin{align*}
    a_{\Delta \Delta} &= \frac{N_1}{N_2} = \frac{V_{AB}}{V_{ab,1s}} \\
    a_{\Delta Y} &= \frac{N_1}{N_3} = \frac{V_{AB}}{\sqrt{3} V_{ab,2s}}
\end{align*}
\]  

(2)

(3)

The secondary winding 1 voltages, \( v_{s1} \), are in phase with the grid voltages, \( v_g \). The secondary winding 2 voltages, \( v_{s2} \), are leading the grid voltages for 30\(^\circ\). As these secondary voltages are applied to the six-pulse rectifiers, \( Rec_1 \) and \( Rec_2 \), the AC power will be rectified. Referring to the power circuit, one of the diodes in the top half of the bridge may conduct as its anode terminal is supplied with highest phase voltage. Consequently, one diode in the bottom half bridge will conduct with its cathode terminal is connected to the lowest phase voltage.

2.2. Eighteen-pulse rectifier transformer

In this paper, authors propose to use a delta-connected primary phase shifting transformer with the secondary windings configured with angle displacement of 0\(^\circ\), −20\(^\circ\), and −40\(^\circ\). This configuration is commonly
used in motor drives applications [14]. Figure 3 (a) illustrates the proposed system configuration in the traction power substation. Three units of six-pulse diode rectifiers are demanded. As shown in the diagram, rectifiers, \( \text{Rec}_1-\text{Rec}_4 \), will be fed with three set of voltages, \( v_{si}, v_{su} \), which are displaced by 20° from each other. All the rectifiers will be connected in parallel like the existing 12-pulse rectifier transformer system.

Each respective connection and phasor diagram of the transformer are presented in Figure 2 (c), Figures 3 (b) and (c). The 0° phase-shift secondary winding terminal generates voltages, \( v_{si} \). These three phase voltages are in-phase with the grid voltages, \( v_p \). The turn ratio for this configuration is presented in (2). On the other hand, the zigzag-connected secondary winding 2 and winding 3 have identical set of coils on primary and secondary sides. As shown in Figure 3 (b) \( N_t \) turns of coils are winded in primary side of the transformer in delta connection. Two set of coils, \( N_t \) and \( N_s \) are winded at secondary side per phase. The \( N_t \) coils are connected in delta, whereas the \( N_s \) coil is connected in series with \( N_t \) coil for each phase. The required phase shifting angles, -20°, and -40° are measured by examining the angle between the primary and secondary line-to-line voltages, \( V_{AB} \) and \( V_{ab,s2} \) or \( V_{ab,s3} \). Thus, by appropriately setting up the turn ratio of \( N_t \), and \( N_s \), the required phase shifting angles can be established. For instance, by evaluating the phasor diagram of Figure 3 (b), the rms voltage across \( N_s \) coil, \( V_q \), and the rms phase voltage between nodes \( a \) and \( n \), \( V_{au,s2} \), can be derived using a triangular composed of \( V_q \), \( V_{bs,s2} \) and \( V_{ab,s2} \).

\[ \frac{v_q}{\sin 20°} = \frac{v_{bs,s2}}{\sin 40°} = \frac{v_{ab,s2}}{\sin 120°} \]

Since a balance three phase voltages is assumed suppling to the transformer, \( V_{bs,s2} \) is equivalent to \( V_{au,s2} \). Therefore, the turn ratio of the secondony windings can be derived as:

\[ \frac{N_s}{N_t+N_s} = \frac{v_q}{v_{au,s2}} = \frac{\sin 20°}{\sin 40°} = 0.5321 \]

Whereas the turn ratio of the primary and secondary windings can be estimated as:

\[ \frac{N_t}{N_s} = \frac{v_q}{v_{si}} = \frac{\sin 20°}{\sin 40°} = 0.5321 \]
\[
a_{\Delta l} = \frac{N_1}{N_4+N_6} = \frac{V_{AU}}{V_{au,s2}} = \frac{V_{AB}}{V_{ab,s2}} \left( \frac{\sin 120^\circ}{\sin 60^\circ} \right) = 1.3473 \frac{V_{AB}}{V_{ab,s2}} \\
\text{where, } V_{AU} = V_{AB} \frac{\sin 60^\circ}{\sin 60^\circ} \text{ and } V_{BV,S2} = V_{au,s2} \frac{\sin 40^\circ}{\sin 120^\circ}
\]

To obtain the \(-40^\circ\) phase shift, the delta connected coils at secondary winding are integrated in a reverse order as shown in Figure 3 (c). With the same derivation steps given in (4)–(6), the identical turn ratio will be determined.

2.3. AC harmonics distortion

With the assumption of a balanced grid voltages are supplied to the traction power substation, the output currents of the phase-shifting transformer for each secondary winding, \(i_{sl}\), can be summarized as:

\[
\begin{align*}
\sum_{n=1}^{n=odd} l_{m,n} \sin \left( n(\omega t + \delta) \right) \\
\sum_{n=1}^{n=odd} l_{m,n} \sin \left( n(\omega t - 120^\circ + \delta) \right) \\
\sum_{n=1}^{n=odd} l_{m,n} \sin \left( n(\omega t - 240^\circ + \delta) \right)
\end{align*}
\]

where \(l_{m,n}\) is the peak value of the \(n\)th order of harmonic current and \(\delta\) represents the displacement angle introduced by the phase-shifting transformer. These currents, \(i_{sl}\), could be referred to primary side of the transformer, \(i'_{sl}\), using the general transformer equation as follows:

\[
i'_{sl} = \frac{1}{a} i_{sl}
\]
Where $a$ represent the transformer turn ratio. In this paper, this parameter could be substituted by (2), (3), or (6) mainly depends on the primary and secondary windings configuration. Thus, the grid current, $i_g$, can be estimated by summing up all referred currents, $i'_1, i'_2$, on the primary windings of the transformer. As shown in (9) and (10) denote idealized phase-a grid current expression for 12-pulse and 18-pulse rectifier transformer system.

$$i_{A,12p} = i'_1 + i'_2$$  \hspace{1cm} (9)

$$i_{A,18p} = i'_1 + i'_2 + i'_3$$  \hspace{1cm} (10)

The details derivation of harmonic current cancellations based on phase displacement of harmonic currents are documented in [14]. Theoretically the grid current harmonics of a $p$-pulse rectifier transformer system should be formulated as:

$$h_{ac} = pk \pm 1 \text{ for } k = 1, 2, 3, \ldots$$  \hspace{1cm} (11)

where $k$ represents an integer. Hence, the most significant harmonics content for a 12-pulse system should be found in the order of 11$^\text{th}$ and 13$^\text{th}$; whereas an 18-pulse rectifier transformer system will locate at 17$^\text{th}$ and 19$^\text{th}$.

As a result, the harmonic distortion is estimated to be minimized using an 18-pulse system based on the Total Harmonic Distortion expression bellows:

$$THD_i = \frac{\sqrt{\sum h_{ac}^2}}{i_{rms}} \times 100\%$$  \hspace{1cm} (12)

Figure 4 shows a set of simulated grid current waveforms for 12-pulse and 18-pulse rectifier transformer systems. The grid currents shown in Figure 4 (a) are more distorted compared to Figure 4 (b).

![Figure 4](image)

Figure 4. Grid current waveforms of the rectifier transformer system for, (a) 12-pulse, (b) 18-pulse

2.4. DC harmonics distortion

By neglecting the commutation inductance, an ideal output voltage waveform, $v_{dc}$, for a $p$-pulse rectifier transformer system could be sketched (Figure 5). Each rectifier will present a line-line voltage across its DC terminal according to one upper and one lower diode conducted at an instant of time period. Thus, $v_{dc}$, can be expressed as:

$$v_{dc} = \sqrt{2}V_{lk} \cos \omega t \text{ for } -\frac{\pi}{p} < \omega t < \frac{\pi}{p}$$  \hspace{1cm} (13)

Where $V_{lk}$ indicates the rms value of the line-line voltages produced by the secondary winding of the transformer. The average output voltage, $V_{dc}$, can be derived as:

$$V_{dc} = \sqrt{2}V_{lk} \left( \frac{2}{p} \right) \sin \frac{\pi}{p}$$  \hspace{1cm} (14)
It is predicted that a 12-pulse and 18-pulse rectifier transformer systems will generate an average output voltage approximate to 1.398\(V_{LL}\) and 1.407\(V_{LL}\) respectively. The output voltage ripple factor can be formulated as:

\[
\frac{\Delta v_{dc}}{v_{dc}} = \left(\cos 0^\circ - \cos \frac{\pi}{P}\right) \times 100\%
\]

Ideally, about 50% of voltage ripple reduction will be achieved by replacing the 12-pulse system with an 18-pulse system. The DC voltage harmonic contents will exist at multiples of the \(P\) pulses as follows:

\[h_{dc} = pk \text{ for } k = 1, 2, 3, \ldots\]

Figure 5. Theoretical output voltage waveform of a \(p\)-pulse rectifier transformer system [21]

3. SYSTEM MODELLING AND SIMULATION VERIFICATION

In order to analyse the power quality of the twelve and eighteen pulses rectifier transformer systems, a DC traction model is built using MATLAB/Simulink as shown in Figure 6 (a). This simulation model is then simulated under rated load condition, using two different set of multipulse rectifier transformer systems (Figures 6 (b), and (c)). Figure 6 (d) shows the power circuit for a 6-pulse rectifier. Three-phase utility grid rated at 33kV line-to-line voltages are integrated as an input supply for the system. Whereas the LRT traction is model as an \(RL\)-load based on the field data documented in [24], [25]. Table 1 summarizes all the simulation parameters used in this paper.

<table>
<thead>
<tr>
<th>Parameters of the multipulse rectifier transformer system [24], [25]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated nominal power and frequency of the transformer, (P_{RX}) and (f)</td>
</tr>
<tr>
<td>Transformer magnetization resistance and inductance</td>
</tr>
<tr>
<td>Rated nominal line-to-line voltage – primary, (V_{p,\text{nom}})</td>
</tr>
<tr>
<td>Rated nominal line-to-line voltage – secondary, (V_{s,\text{nom}})</td>
</tr>
<tr>
<td>Traction network (RL)-load</td>
</tr>
</tbody>
</table>

Figure 7 presents the simulated grid voltages and currents waveforms. The simulation results of 12-pulse rectifier transformer system are compiled in column (a) while column (b) reserved for 18-pulse rectifier transformer system. Sub-plot i. show that identical voltage supplies are implemented for both simulations. The three phase voltages are balance with its peak voltage set at 26.94 kV, 50 Hz. Sub-plot ii. present the simulated three phase grid currents waveforms and sub-plot iii capture the harmonic spectrum of phase-a grid current.

As shown in Figure 7 (a) ii. and iii., a 12-pulse rectifier transformer system draws an effective current of approximately 56.01 A to power up the LRT railway. The Total Harmonic Distortion (THD) are recorded less than 5%, which fulfilled the IEEE Standard requirement. Its most significant harmonics contents are measured at 11th, 13th, 23rd, and 25th orders, which fulfilled the theoretical expression given in (11). The grid current waveforms shown in Figure 7 (b) ii. are obviously more sinusoidal compared to the 12-pulse system. The effective current drawn by an 18-pulse rectifier transformer system is slightly higher, which is about 59.76 A. The current harmonis distortion is reduced to 3.69%. However, additional harmonic contents are recorded in the harmonic spectrum at the order of 5th, 7th, 11th, and 13th (as highlighted in Figure 7 (b) iii.). This simulation result does not comply with the theoretical formulation of ac harmonics equation. Therefore, further investigation is conducted by examining the 18-pulse phase-shifting transformer secondary windings.
Phase-a current waveforms for each secondary winding are compiled in Figure 8. Figure 8 (a) illustrates current waveform of the delta connected secondary winding, $i_{s1}$. Since the secondary winding is in phase with primary winding of the transformer, a typical 6-pulse rectifier (RL-load) source current waveform is obtained. The effective current of this simulated waveform is calculated as 1154.0 A with its THD is captured at 31.27%. This current waveform contains odd harmonics except trippen harmonic orders which complies to the theoretical 6-pulse rectification system. The most significant harmonic located at 250 Hz ($5^{th}$ order) with an amplitude of approximately 30% of its fundamental component. Figure 8 (b) shows the secondary winding ac current waveform of the zigzag transformer set with -20° phase displacement, $i_{s2}$. This current waveform is badly distorted, which contains odd number of harmonic components. The measured THD, is noted at 93.88%. The effective current of $i_{s2}$ is computed as 804.4 A. Lastly, Figure 8 (c) depicts another zigzag transformer current waveform with the displacement angle set to -40°, $i_{s3}$. The rms current and THD of $i_{s3}$ is simulated as 1703 A and 30.88%.

In summary, those additional harmonic contents of the grid current (as highlighted in Figure 7 (b) iii.) are resulted from the badly distorted current waveforms produced in the zigzag transformers. The displacement angles, -20° and -40°, selected for the phase-shifting transformer in this paper fails to achieve the harmonic cancellation theory [14].

Figure 6. These figures are; (a) Simulation model of multipulse rectifier transformer, (b) 12-pulse rectifier transformer configuration with $\Delta/\Delta$ (0°) and $\Delta/Y$ (30°), (c) 18-pulse rectifier transformer configuration with $\Delta/\Delta$ (0°), $\Delta/Z$ (-20°) and $\Delta/Z$ (-40°), (d) power circuit of 6-pulse rectifier.
Figure 7. Simulation results for rectifier transformer (a) 12-pulse; (b) 18-pulse. The sub-plots show: i. Phase voltage waveforms, ii. Line current waveforms, iii. Harmonic spectrum of phase-a line current waveform

Figure 8. Phase-a secondary winding current waveform of 18-pulse rectifier transformer system: (a) $i_{s1}$ [$\Delta\Delta$ ($0^\circ$)], (b) $i_{s2}$ [$\Delta\Delta$ ($-20^\circ$)], and (c) $i_{s3}$ [$\Delta\Delta$ ($-40^\circ$)]

In Figure 9 shows the rectified DC voltages and current waveforms for both rectifier transformer systems. The simulation results prove that 18-pulse rectifier system offers better DC voltage and current quality compared to the 12-pulse system. The FFT results presented in Figure 10 (a) shows that the average DC voltages are computed as 744.2 V and 758.6 V for 12-pulse and 18-pulse systems. As compare, the voltage ripples have been further reduced for 20 V with the application of 18-pulse rectifier system. On the other hand, the DC current shows an increment of about 77 A. Besides, the current ripple is also further minimized for about 13 A. Both current and voltage ripple factors do not achieve 50% reduction mainly due to this simulation taking into account the inductive load for analysis. The DC voltage and current harmonics contents for the 12-pulse rectification system is found at $12^{th}$, $24^{th}$, and $36^{th}$ orders following the theoretical formulation. Unfortunately, the 18-pulse system DC voltage and current harmonics exist in order of six-multiplication. These additional harmonic contents as highlighted in Figure 10 (b) are mainly affected by highly distorted secondary transformers currents, $i_{s2}$, and $i_{s3}$. 

DC traction power substation using eighteen-pulse rectifier transformer system (Chuen Ling Toh)
4. CONCLUSION

The potential of implement an 18-pulse rectifier transformer in LRT traction power substation has been investigated. This paper had proposed to use a phase-shifting transformer which had been widely used in motor drive applications. The primary winding of the transformer is configured in delta connection, whereas the secondary winding of the transformer is winded in delta and zigzag configurations to form respective displacement angles of 0°, -20°, -40°. The fundamental concept of 12-pulse and 18-pulse phase-shifting transformer had been presented in detail with ac and DC harmonics formulation. The proposed system had been modelled and simulated to evaluate its feasibility. The simulation results prove that further mitigation of about 1.22% ac current harmonic distortion had been achieved. In addition, the DC voltage and current ripple may also be further reduced for about 30%. However, the harmonics contents for the proposed 18-pulse rectifier transformer does not match with the theoretical formulation. It is found that those additional harmonics orders mainly contributed by the zigzag secondary windings of the phase-shifting transformer.
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