Detailed modeling of two diode photovoltaic module using MATLAB simulik

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Article Info	ABSTRACT
Article history:	This paper proposes an accurate model of Photovoltaic Module. The model is
Received Nov 10, 2018 Revised Feb 12, 2019 Accepted Apr 10, 2019	presented in details and simulated by Matlab Simulink. The PV module is presented as a two diode model with the series' and parallels' resistances. The method is used to obtain the parameters of the module by using data provided by the manufacturer. To verify the accuracy of the proposed model, a comparison is done between the present results and those in a previous paper in which the single diode detailed model was studied. The same type of modules (PWX 500) is used to compare and validate results. The weather
Keywords:	
Two diode model DC/DC converter MPPT Duty cycle Matlab/Simulink	data as illumination and temperature are taken as input variables when current and Power are output variables. For the validation of the proposed model, it is used to power a resistive load by using a boost converter controlled by à Maximum Power Point Tracking method. The proposed method is very detailed and can be useful for PV researchers for their works
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1. INTRODUCTION

Electricity generated from fossil fuels which are based on oil and gas represents more than 60% of the world production. Until today, it remains the basis for electricity production. But it is also the first source of pollution. In addition to this, the traditional organization of the electrical system (production, transport, distribution) is seen over the decades, attenuated because of two key phenomena; population growth and change of the load quality which contains now more polluting devices such as computing devices for example.

Renewable energy is needed nowadays as an alternative to fossil energy in depletion. Repetitive natural phenomena as sunlight, wind and wave offer to us a very good opportunity to recover the clean aspect of our planet. In recent decades, many researchers are working on the PV cell technology and its efficiency. The electric power generated by the PV module depends strongly on irradiance and temperature.

The photovoltaic cell is the basic device which generates electricity from sunlight. Cells are grouped in series to increase voltage or in parallel to increase current. Modules and arrays are formed by the cited association of cells. The PV cell is presented by an equivalent circuit elaborated according to the fundamentals of semi conductors. The simplest model is an ideal equivalent circuit made of a current source in parallel with a diode as shown in Figure 1 [1] and which doesn't take in consideration many parameters related to fabrication processes or to the materials

A practical model includes a resistance Rs in series with the current source as in [2-6]. Rs is responsible for the reduction in output voltage [7]. However, this model exhibits serious deficiencies when subjected to temperature variations. A most practical model adds another resistance R_p in parallel with the diode as in [7-11]. R_P reduces the output current of the module because of the leakage current through the

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parallel branch [7]. But the most accurate model is the Two Diode $R_s R_p$ model [12, 13] as shown in Figure 2.



Figure 1. PV cell equivalent circuits [1]

Figure 2. Two Diode model of PV cell

As manufacturers don't give enough information on data sheets about the parameters which depend on weather conditions (illumination and temperature), some assumptions are necessary to establish a mathematical model of the PV cell and the PV module. After modeling the PV cell, the optimal power can be determined accurately with the mathematical model so that it matches with the experimental data. I(V) characteristic is a non-linear (Transcendental) equation with several parameters. Some of them are provided by constructors but have to be adjusted, and others must be computed in the present work as R_P , reverse saturation currents of the two diodes I_{S1} and I_{S2} , and their ideal factors A_1 and A_2 . The objective of our work is to determine the parameters and simulate the module with these settings in order to compare the power generated by simulation with the one obtained experimentally and delivered by the constructor. Then, the PV module is connected with a load via a DC/DC converter

2. PRESENTATION AND MODELING OF PV MODULE

2.1. One Diode PV model

The red part of Figure 1 shows that the Kirchhoff law allows obtaining the output current I for the ideal model:

$$I = I_{ph} - I_d \tag{1}$$

Where I_{ph} is the photocurrent, I_d the Diode current which is given by (2):

$$I_d = I_s \left[e^{\frac{V}{A.N_s.V_T}} - 1 \right] \tag{2}$$

Where V is the voltage imposed to the diode, V_T the thermal voltage and equal to (k.T_C/q), T_C is the cell temperature in Kelvin (K), k is the Boltzmann constant (1,381.10⁻²³j/K), q is electron charge (1.602.10⁻¹⁹C), Ns is the number of cell connected in series, A the ideality factor and I_s the reverse saturation current.

The presence of the series resistance changes the diode current into the following form:

$$I_d = I_s \left[e^{\frac{q(V+I.R_s)}{A.N_s.k.T_c}} - 1 \right]$$
(3)

The bleu part of Figure 1 shows the most practical One Diode model. The output current is also obtained by Kirchhoff law and written in (4):

$$I = I_{ph} - I_d - I_p \tag{4}$$

Where I_P is the current of leak in parallel resistance R_P .

According to the previous equation, the output current of the One Diode module with N_{S} cells in series is:

$$I = I_{ph} - I_s \left[e^{\frac{q(V+I,R_s)}{AN_s,k,T_c}} - 1 \right] - \frac{V+IR_s}{R_p}$$
(5)

2.2. Two Diode PV model

The most accurate model is presented in Figure 2. It is also called "Two exponentials model". It is given as:

$$I = I_{ph} - I_{s1} \left[e^{\frac{q(V+I.R_s)}{A_1.N_s.k.T_c}} - 1 \right] - I_{s2} \left[e^{\frac{q(V+I.R_s)}{A_1.N_s.k.T_c}} - 1 \right] - \frac{V+IR_s}{R_p}$$
(6)

3. DETERMINATION OF THE PARAMETERS

Seven parameters must be determined I_{ph} , I_{S1} , I_{S2} , R_s , R_p , A_1 , and A_2 . But as A_1 and A_2 are assumed, I_{S1} and I_{S2} are not determined and Iph is known, the parameters to be determined are only R_s and R_p - The photocurrent under any conditions depends on irradiance and temperature and $I_{ph,ref}$:

$$I_{ph} = \frac{G}{G_{ref}} (I_{ph,ref} + k_i.\Delta T)$$
⁽⁷⁾

Where $I_{ph,ref}$ (A) is the photocurrent at STC and G is the Irradiance called also illumination (W/m²), G_{ref} : Irradiance at STC = 1000W/m², $\Delta T = T_c - T_{c,ref}$ (Kelvin), $T_{c,ref}$ is the cell temperature at STC = 25+273=298K, k_i is the coefficient temperature of short circuit current (A/K), provided by the manufacturer.

- The reverse saturation current for each diode is given by the following expressions[19]:

$$I_{s1} = I_{sc,ref} \cdot exp\left(\frac{-q.V_{oc,ref}}{A_1.N_s.k.T_c}\right) \left(\frac{T_c}{T_{c,ref}}\right)^3 exp\left[\left(\frac{q.\varepsilon_G}{A_1.k}\right) \left(\frac{1}{T_{c,ref}} - \frac{1}{T_c}\right)\right]$$
(8)

$$I_{s2} = I_{sc,ref} \cdot exp\left(\frac{-q.V_{oc,ref}}{A_2.N_S.k.T_c}\right) \left(\frac{T_c}{T_{c,ref}}\right)^3 exp\left[\left(\frac{q.\varepsilon_G}{A_2.k}\right) \left(\frac{1}{T_{c,ref}} - \frac{1}{T_c}\right)\right]$$
(9)

- A1 is the ideality factor of the first diode according to the diffusion current densities.

- A₂ is the ideality factor of the second diode according to recombination current density [17].

Most of papers on two diode model of PV cell assumed that $A_1 = 1$ and $A_2 = 2$ [7, 8, 13].

In the proposed model, $A_1 = 1$ and $A_2 = 1.2$ because when plotting P(V) characteristics, the best match is obtained with the practical model provided in manufacturer data sheet [14-18], and (6) is now rewritten at maximum power condition (according to data sheet):

$$I_{\max,ref} = \frac{P_{\max,ref}}{V_{\max,ref}} = I_{ph,ref} - I_{d1} - I_{d2} - \left[\frac{(V_{\max,ref} + R_s.I_{\max,ref})}{R_p}\right]$$
(10)

 R_S is varied to compute R_P in (6) which is implemented in Matalb Simulink environment. The iteration starts at $R_S = 0$ and increases in order to force the computed max power point moving until it matches with the experimental max power point. The corresponding R_P is then deduced. Finally, only one pair (R_P , R_S) satisfies this condition and its expression at max power is written as follows:

$$R_{p} = \frac{V_{max,ref} + R_{s}.I_{max,ref}}{I_{ph,ref} - I_{s1} \left[e^{\frac{q(V+I.R_{s})}{A_{1}.N_{s}.k.T_{c}}} - 1 \right] - I_{s2} \left[e^{\frac{q(V+I.R_{s})}{A_{1}.N_{s}.k.T_{c}}} - 1 \right] - \frac{P_{max,ref}}{V_{max,ref}}$$
(11)

The PWX 500 PV module (49W) is used to validate the proposed model. The series resistance R_s is provided equal to 0.55Ω but R_P is not given as seen in Table 1. Results of the One Diode Model, previously given in detail in [19], are given now in table to be compared with results of the Two Diode Model and with the provided data at STC.

Table 1. PWX 500 PV module (49W) characteristics at 25 °C, 1.5AM, 1000W/m²

	Provided parameters	Adjusted parameters for	Adjusted parameters for
	_	One Diode Model	Two Diode Model
P max	49 W	49 W	49 W
I_{mp}	2.88 A	2.88 A	2.88 A
V _{mp}	17 V	17 V	17 V
Isc	3.11 A	3.11 A	3.11 A
V _{oc}	21.8 V	21.8 V	21.8 V
Rs	0.55 Ω	0.45 Ω	0.3 Ω
R _P	-	310 Ω	200 Ω
A_1	-	1.3	1
A_2	-	-	1.2
I_{S1}	-	4.116*10 ⁻⁸ A	1.782*10 ⁻¹⁰ A
Is2	-	-	9.075*10 ⁻⁹ A
Noct	45 C°	45 C°	45 C°
\mathbf{K}_{i}	1.3*10-3 (/K°)	1.3*10-3 (/K°)	1.3*10-3 (/K°)
K_v	-72.5*10-3(/K°)	-72.5*10-3(/K°)	-72.5*10-3(/K°)
N_s	36	36	36

4. SIMULATION OF THE PROPOSED MODEL

Figure 3 represents the main system. Input variables are Temperature and Irradiance when output variables are Current delivered by the module and power generated to be used by load either in stand alone or grid connected mode. Figure 4 is a subsystem of the main system. It is an implementation of (6). It is used to simulate the proposed model by incrementing R_s until matching P_{mp} with $P_{mp,ex}$. The experimental data for maximum power at STC provided by the manufacturer of PWX 500 PV module (49W) are given in Table 1.

To valid our model, the PV module is simulated under Matlab-Simulink. The general diagram is given in Figure 5. It comprises of a PV module and a resistive load in parallel. A diode is connected in series to prevent the reverse current flow. To make the voltage stable, a filter is connected before the load. A converter is used to boost voltage. Its gate is controlled by the output of MPPT (Maximum Power point Technique) bloc in order to get the max of the power delivered by the PV module.

One of the most used methods of algorithms in MPPT is Perturb and Observe commonly called (P&O). It consists on making a perturbation in the voltage and observing the rate of change of power. It depends on the position of the optimum point to adjust the reference voltage [20]. A flowchart of P&O method is presented in Figure 6.



Figure 3. Presentation of the whole PV model



Figure 4. Detailed Two Diode model with RP



Figure 5. General diagram of Photovoltaic system connected to a resistive load



Figure 6. The flowchart of P&O algorithm

The duty cycle can control the DC/DC converter and maintain the voltage at the maximum. The diagram of Figure 7 taken from references [21] and [24] presents a part of our main system concerning the DC/DC converter built a high frequency IGBT switch. Authors give equations of inductor (L), capacitor (C) and the duty cycle (D):

$$L = \frac{v_{int}.D.T}{\Delta i_L} ; \quad C = \frac{V_{in}.D.T}{\Delta V_0.R.f} ; \quad D = \frac{V_{out} - V_{in}}{V_{out}}$$

Where here, Δi_L indicates inductor ripple current and ΔV_0 indicates capacitor voltage ripple, T is the time period (sec) and f the switching frequency (Hz)



Figure 7. Circuit Diagram for Boost Converter [21, 24]

5. RESULTS AND ANALYSIS

In a previous work [19], the One Diode R_P model was modeled and simulated under Matlab environment. The series resistance R_S was adjusted to 0.45 Ω instead of 0.55 Ω provided by manufacturer and the parallel resistance was computed iteratively and equal to $R_P = 310 \Omega$ (not provided). The module PWX 500 (49W) was used to validate results. In the present work, the same method is used to adjust R_S and compute R_P for the Two Diode Model. Adjusted and computed parameters are summarized in Table1.

 R_S is iteratively increased and R_P is simultaneously computed. The iterative method gave $R_S = 0.3\Omega$ and $R_P = 200\Omega$. These two values make the two diode model most representative for the chosen PV module. To simulate any other PV module, one can introduce in the (19) the respective experimental maximum power and then, the iterative method is used to determine the appropriate pair (R_S , R_P) which makes the model the most representative.

After running simulation for some different values of R_s , I-V curves of are represented in Figure 8, and P-V in Figure 9. One can say in Figure 8, that the shape moves to the rectangular form when R_s decreases. I_{sc} and V_{oc} are not affected by change of R_s , so the fill factor which is given by (12) change only with P_{mp} :

$$FF = \frac{P_{mp}}{V_{oc}I_{sc}} \tag{12}$$

This is in accordance with (11) where P_{mp} is with respect of R_S and R_P .

When comparing the One Diode model curves and the Two Diode model ones as shown in Figures 10 and 11, one can say thatfor the first model, simulated curves match with experimental data at $R_S = 0.45\Omega$ and $R_P = 310\Omega$. For the second model, simulated curve match with experimental data at $R_S = 0.3\Omega$ and $R_P = 200\Omega$.



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The proposed model can be used to simulate PV module at different levels of irradiance and temperature The I (V) and P (V) characteristics are respectively presented in Figure 12 and Figure 13, by varying irradiance from 200W/m² to 1000 W/m² at T =25°C. In Figure 13 and Figure 14, The I (V) and P (V) characteristics are respectively presented by varying temperature from 0°C to 60°C at G =.1000 W/m². In Figure 14 and Figure 15, The I (V) and P (V) characteristics are respectively presented by varying temperature from 0°C to 60°C at G =.1000 W/m².



Figure 12. I (V) characteristics by varying irradiance at $T=25^{\circ}C$



Figure 14. I (V) characteristics by varying temperature at G=1000W/m²



Figure 13. P (V) characteristics by varying irradiance at $T=25^{\circ}C$



Figure 15. P (V) characteristics by varying temperature at G=1000W/m²

The next step of the work is to use the proposed model in the topology presented in Figure 5. The one stage PV system adaptation is used to supply a resistive load. Since the one stage system is in continuous current mode, voltage and current at DC/DC converter (load side) are given by [22]. In the reference [23], the duty cycle D is taken as α and η is the efficiency of the boost converter:

$$V_L = \frac{v_{pv}}{1-D} \tag{13}$$

$$I_D = \eta (1 - D) I_{pv} \tag{14}$$

Figure 15 shows the simulation of power delivered to the load by varying irradiance at 1s from 400W/m² to 1000W/m² and from 1000W/m² to 400W/m² at 3s in the general diagram is given in Figure 5 when using P&O algorithm. One can see that when varying irradiance, the power delivered to the load corresponds to the maximum power extracted to the module at each level according to the plots presented in Figure 13.



Figure 15 Power delivered to the load with P&O method

6. CONCLUSION

In this paper, an accurate model of PV cell is presented in details and simulated under MATLAB/SIMULINK environment. Elaboration of the presented model is in accordance with the fundamentals of semi conductors and the technology of the PV cell. The computed parameters of the PV cell are chosen because of their variation with irradiance and temperature. This model can be used as a tool to study all type of PV modules available in markets even if manufacturers don't give all parameters. The series resistance R_s, is adjusted by increasing from zero and used to compute the parallel resistance in order to match the experimental maximum power point provided in data sheet with the computed one. In our case, a pair of $(R_s = 0.3\Omega, R_p = 200 \Omega)$ instead of $(R_s = 0.55\Omega, and R_p \text{ not provided})$ is obtained and then to simulate and validate the proposed model. In a previous work, a single diode R_P model was presented and this work about Two Diode Model is a new step. Then, the proposed model was simulated in a general diagram a resistive load via a continued bus. A DC/DC boost converter was used and controlled by an MPPT (Maximum Power Point Tracker) method. The chosen algorithm was P&O because it's easily implemented. The accuracy of the proposed model is demonstrated by different plots which show that the power delivered to load match with the maximum power obtained from the PV module. In this work, the simplest form of load was used to explain and illustrate the proposed model. A possible future application of this model will be in grid connected PV system with a non linear load.

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