# A Performance Comparison of DFIG using Power Transfer Matrix and Direct Power Control Techniques

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| Article Info   | ABSTRACT   |
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| Article history:<br>Received Mar 13, 2014  | This paper presents a direct power control and power transfer matrix model<br>for a doubly-fed induction generator (DFIG) wind energy system (WES).<br>Control of DFIG wind turbine system is traditionally based on either stator-  |
| Accepted Jul 2, 2014   | flux-oriented or stator-voltage-oriented vector control. The performance of<br>Direct Power Control (DPC) and Power transfer Matrix control for the same<br>wind speed are studied. The Power transfer matrix Control gave better  |
| <i>Keyword:</i><br>Doubly-fedInduction generator<br>(DFIG)<br>Direct Power control (DPC) | results. The validity and performance of the proposed modelling and control approaches are investigated using a study system consisting of a grid connected DFIG WES. The performance of DFIG with Power Transfer Matrix and Direct Power Control (DPC) techniques are obtained through simulation. The time domain simulation of the study system using MATLAB Simulink is carried out. The results obtained in the two cases are compared. |
| Power Transfer Matrix<br>Pulse width modulation (PWM)<br>Wind energy                     | Copyright © 2014 Institute of Advanced Engineering and Science.<br>All rights reserved.  |
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# 1. INTRODUCTION

Generation of electricity has been largely dominated by nuclear, hydro and fossil-fueled thermal plants. Generally this type of generation is considered as conventional power generation. The main drawback of most conventional power plants is the adverse impact on the environment. The gradual depletion of fossil-fuel (such as coal, gas) reserves is also a concern. The solution to these problems lies in adopting non-conventional methods such as wind, solar etc. in power generation. Wind is regarded as the best suitable renewable energy resource for production of power and the best alternative to the conventional energy resources mainly because of availability of large wind turbines [1].

For the last two decades, research is being carried out specifically on Wind Energy Systems to capture more power at fluctuating wind speeds. With the improvement in the power electronic technology constant speed constant frequency (CSCF) generators were replaced by variable speed constant frequency (VSCF) generators in WES. The Doubly Fed Induction Generator (DFIG) is currently the choice of generator for multi-MW wind turbines .The aerodynamic system must be capable of operating over a wide wind speed range in order to achieve optimum aerodynamic efficiency by tracking the optimum tip-speed ratio.Therefore, the generator's rotor must be able to operate at a variable rotational speed. TheDFIG system, therefore operates in both sub- synchronous and super-synchronous modes with a rotorspeed range around the synchronous speed. The stator circuit is directly connected to thegrid while the rotor winding is connected via slip-rings to a three-phase converter. Forvariable - speed systems where the speed range requirements are small, (for example  $\pm 30\%$  ofsynchronous speed) the DFIG offers adequate performance and is sufficient for the speedrange required to exploit typical wind resources.

The doubly fed induction generator (DFIG) based wind turbine with variable speed and variable pitch control scheme is the most popular wind power generation system in the wind power industry. This

machine can be operated either in grid connected mode or in standalone mode. This system has recently become very popular as generator for variable speed wind turbines. The major advantage of the doubly fed induction generator (DFIG), which has made it popular, is that the power electronic equipment has to handle only a fraction (20-30%) of the total system power [2], [3]. That means the losses in the power electronic equipment can be reduced in comparison to power electronic equipment that has to handle the total system power as for a direct-driven synchronous generator, apart from the cost saving of using smaller converters. Control of the DFIG is more complicated than the control of a standard induction machine. In order to control the DFIG rotor current is controlled by a power electronic converter. One common way of controlling the rotor current is by means of Field oriented (vector) control. Direct torque control (DTC) of induction machines, provides an alternative to vector control [5]. Based on the principles of DTC strategy, direct power control (DPC) was developed for three-phase pulse width modulation (PWM) converters.

Power transfer matrix is a control technique of DFIG which uses instantaneous real and reactive power instead of dq components of currents in a vector control scheme. The main features of the proposed model compared to conventional models in the dq frame of reference are [6].

a) Robustness: The waveforms of power components are independent of a reference frame; therefore, this approach is inherently robust against unaccounted dynamics such as PLL.

b) Simplicity of realization: The power components (state variables of a feedback control loop) can be directly obtained from phase voltage/current quantities, which simplify the Implementation of the control system.



Figure 1. Structure of DFIG wind power generating system

### 2. WIND TURBINE MODEL

The wind turbine characteristics must be analyzed for getting optimum power curve ( $P_{opt}$ ). The power output of Wind turbine is given by [4]:

$$P_0 = C_p * P_V = 0.5 \rho S_w V^3 C_p$$
(1)

Where ' $\rho$ ' is the air density; S<sub>w</sub> is wind turbine blade swept area in the wind, V is wind speed. C<sub>p</sub> represents the power conversion efficiency of the wind turbine. It is a function of  $\lambda$  (Tip-speed Ratio).

$$\lambda = \frac{2\pi RN}{V\infty} = \frac{R}{V}\omega \tag{2}$$

Where 'R' is the blade radius;  $\omega$  is the angular velocity of the rotating blades; N is the rotational speed in revolutions per second, and V<sub> $\infty$ </sub> is thewind speed without the interruption of rotor. C<sub>p</sub> can be calculated by using the formula:

$$C_{p}=0.5716^{*}(\frac{1}{\lambda i}) (116^{*}-0.4\beta-5)^{*}e[-21\left(\frac{1}{\lambda i}\right)] + 0.068^{*}\lambda$$

$$\frac{1}{\lambda i} = \frac{1}{\lambda + 0.08\beta} - \frac{0.035}{\beta^{3} + 1}$$
(3)

Maximum power from the wind turbine is:

$$P_{max} = K \omega^3$$
(4)

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Where  $k = 0.5 S_w \left(\frac{\lambda opt}{R}\right)^3 * C_p$ 

# **3. DIRECT POWER CONTROL OF DFIG**



Figure 2. Equivalent circuit of DFIG in the synchronous d-q reference frame



Figure 3. Stator and rotor flux vectors in synchronous d-q frame

The equivalent circuit of a DFIG in the synchronous d-qframe, rotating at the speed of  $\omega_1$ , is shown in Figure 2. The d-axis of the synchronous frame is fixed to the stator flux, as shown in Figure 3. With reference to Figure 2, the stator voltage vector in the synchronous d-q reference frame is given as:

$$V_{s}^{s} = R_{s} I_{s}^{s} + (d\Psi_{s}^{s}/dt) + j\omega_{1}\Psi_{s}^{s}$$
(5)

Under balanced ac voltage supply, the amplitude and rotating speed of the stator flux are constant. Therefore, in the synchronous d-q frame, the stator flux maintains a constant value [5]. Thus;

$$\Psi_{s}^{s} = \Psi_{sd}$$

$$(d\Psi_{s}^{s}/dt) = 0$$
(6)

Considering Equation (5) and neglecting the voltage drop across the statorresistance, Equation (6) can be simplified as:

$$\mathbf{V}_{s}^{s} = \mathbf{j}\boldsymbol{\omega}_{1} \,\boldsymbol{\Psi}_{s}^{s} = \mathbf{j}\boldsymbol{\omega}_{1} \boldsymbol{\Psi}_{sd} \tag{7}$$

The stator current in the synchronous d-q frame is given as:

$$I_s^s = \frac{L_r \psi_s^s - L_m \psi_r^s}{L_s L_r - L_m^2} = \frac{\psi_s^s}{\sigma L_s} - \frac{L_m \psi_r^s}{\sigma L_s L_r}$$
(8)

Thus the stator active and reactive power inputs can be calculated as:

$$P_{s} - jQ_{s} = 3/2 j\omega_{l}\psi_{sd} \times \left(\frac{\psi_{s}}{\sigma}L_{s} - \frac{L_{m}\psi_{r}}{\sigma}L_{s}L_{r}\right)$$

$$P_{s} - jQ = 3/2 j\omega_{l}\psi_{sd} \times \left(\frac{\psi_{sd}}{\sigma}L_{s} - \frac{L_{m}(\psi_{rd} - j\psi_{rq})}{\sigma}L_{s}L_{r}\right)$$

$$P_{s} - jQ_{s} = k\sigma\omega_{l}\left[-\psi_{sd}\psi_{rq} + j\psi_{sd}\left(\frac{L_{r}\psi_{sd}}{L_{m}} - \psi_{rd}\right)\right]$$
(9)

Splitting Equation (9) into real and imaginary parts yields:

$$P_{s} = -k_{\sigma}\omega_{1}\psi_{sd}\psi_{rq}$$

$$Q_{s} = k_{\sigma}\omega_{1}\psi_{sd}\left(\psi_{rd} - \frac{L_{r}}{L_{m}}\psi_{sd}\right)$$
(10)

$$\Delta P_s = -K_{\sigma} \omega_1 \psi_{sd} \Delta \psi_{rq}$$

$$\Delta Q_s = K_{\sigma} \omega_1 \psi_{sd} \Delta \psi_{rd}$$
(11)

Equation (10) indicates that the stator reactive and active power changes are determined by the changes of the rotor flux components on the d-q axis, i.e.,  $\Delta \Psi r d$  and  $\Delta \Psi r q$ , respectively.

# 4. ACTIVE AND REACTIVE POWER CONTROL

The active and reactive power control calculates the required rotor voltage that will reduce the active and reactive power errors to zero during a constant sampling time period of Ts. A PWM modulator is then used to generate the applied rotor voltage for the time period of Ts.

Within the time period of Ts, the rotor voltage required to eliminate the power errors in d-q reference frame are calculated as [7]-[9]:

$$V_{rd} = \frac{1}{T_s} \frac{\Delta Q_s}{k_\sigma \omega_l \psi_{sd}} - \omega_s \psi_{rq}$$

$$V_{rq} = \frac{1}{T_s} \frac{-\Delta P_s}{k_\sigma \omega_l \psi_{sd}} + \omega_s \psi_{rd}$$
(12)

However, its accuracy could be affected by the variation of Lm (Mutual inductance). An alternative method based on Equation (11) gives:

$$\psi_{rd} = \frac{Q_s}{k_{\sigma} \omega_1 \psi_{sd}} + \frac{L_r}{L_m} \psi_{sd}$$

$$\psi_{rq} = \frac{-P_s}{k_{\sigma} \omega_1 \psi_{sd}}$$
(13)

From the Equation (12) and (13) we get:

$$V_{rd} = \frac{1}{T_s} \frac{\Delta Q_s}{k_\sigma \omega_1 \psi_{sd}} + \omega_s \frac{P_s}{k_\sigma \omega_1 \psi_{sd}}$$

$$V_{rq} = \frac{1}{T_s} \frac{-\Delta P_s}{k_\sigma \omega_1 \psi_{sd}} + \omega_s \left(\frac{Q_s}{k_\sigma \omega_1 \psi_{sd}} + \frac{L_r}{L_m} \psi_{sd}\right)$$
(14)

The first terms on the right hand side reduce power errors while the second terms compensate the rotor slip that causes the different rotating speeds of the stator and rotor flux.



Figure 4. Schematic diagram of the DPC for a DFIG system

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# 5. PRINCIPLES OF POWER TRANSFERMATRIX

The schematic diagram of a DFIG wind turbine generator is represented in Figure 1. The power Converter includes Rotor-side-converter (RSC) to control speed of the generator and Grid-side converter (GSC) to inject reactive power to the system. The instantaneous real and reactive power components of the grid side converter,  $p_g(t)$  and  $q_g(t)$  in the synchronous d-q frame of reference are [6]:

$$\begin{bmatrix} p_g(t) \\ q_g(t) \end{bmatrix} = \frac{3}{2} \begin{bmatrix} v_{sd} & v_{sq} \\ v_{sq} & -v_{sd} \end{bmatrix} \begin{bmatrix} i_{gd} \\ i_{gq} \end{bmatrix}$$
(15)

# 6. MODEL OF DFIG USING INSTANTANEOUS POWER COMPONENTS

The change in real power and reactive power can be expressed as [12]-[14]:

$$\frac{dp_s}{dt} = g_1 p_s - \omega_{sl} q_s - g_4 \psi_{sd} - g_5 \psi_{sq} + u_{rd}$$

$$\frac{dq_s}{dt} = \omega_{sl} p_s + g_1 q_s + g_4 \psi_{sq} - g_5 \psi_{sd} + u_{rd}$$
(16)

Where,

$$u_{rd} = g_{2}v_{rd} + g_{3}v_{rq} - 3\frac{v_{s}^{2}}{2L_{s}^{2}}$$

$$u_{rq} = g_{3}v_{rd} - g_{2}v_{rq}$$

$$g_{1} = -\frac{r_{s}L_{r} + L_{s}r_{s}}{L_{s}L_{r}}; g_{2} = \frac{3L_{m}v_{sd}}{2L_{s}L_{r}}$$

$$g_{3} = \frac{3L_{m}v_{sq}}{2L_{s}L_{r}}$$

$$g_{4} = \frac{3}{2} \left(\frac{r_{r}v_{sd} - L_{r}\omega_{r}v_{sq}}{L_{s}L_{r}}\right)$$

$$g_{5} = \frac{3}{2} \left(\frac{r_{r}v_{sd} + L_{r}\omega_{r}v_{sq}}{L_{s}L_{r}}\right)$$
(17)

The electromechanical dynamic model of the machine is:

$$\frac{d\,\omega_r}{dt} = \frac{P}{J} \left( T_e - T_m \right) \tag{18}$$

Where P,J and Tm are the number of pole pairs, inertia of therotor, and mechanical torque of the machine, respectively. Theelectric torque is given by [10], [11]:

$$T_{e} = \frac{3}{2} P\left(\psi_{sd} i_{sq} - \psi_{sq} i_{sd}\right)$$
(19)

$$\frac{d\omega_r}{dt} = g_6 p_s + g_7 q_s - \frac{P}{J} T_m$$
<sup>(20)</sup>

Where,

$$g_{6} = \frac{P^{2}}{J} \frac{\psi_{sq} v_{sd} - \psi_{sd} v_{sq}}{v_{s}^{2}}$$

$$g_{7} = \frac{P^{2}}{J} \frac{\psi_{sd} v_{sd} + \psi_{sq} v_{sq}}{v_{s}^{2}}$$
(21)



Figure 6. Schematic diagram of the study system of power transfer matrix

# 6. RESULTS AND COMPARISION

The following parameters are used to verify the real power, Reactive power and dc link voltages:

| Parameters                                 | Values | Units |
|--|--------|-------|
| Rated power(P)                             | 1.5    | MW    |
| Rated voltage(V)                           | 0.575  | KV    |
| Rated frequency(F)                         | 60     | Hz    |
| Rated wind speed(V <sub>w</sub> )          | 12     | m/s   |
| Stator resistance(R <sub>s</sub> )         | 1.4    | mΩ    |
| Rotor resistance(R <sub>r</sub> )          | 0.99   | mΩ    |
| Stator leakage inductance(L <sub>S</sub> ) | 89.98  | μH    |
| Rotor leakage inductance(L <sub>R</sub> )  | 82.08  | μH    |
| Magnetizationinductance(L <sub>m</sub> )   | 1.526  | mH    |
| Stator/rotor turns ratio                   | 1      | -     |
| Poles                                      | 6      | -     |
| Turbine rotor diameter                     | 70     | М     |
| Lumped inertia constant                    | 5.05   | S     |









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Figure 8(b). Reactive power from power transfer matrix control



Figure 9(a). Real power from DPC



Figure 9(b). Reactive power from DPC



Figure 10(a). Vdc from Power transfer matrix



Figure 10(b). Vdc from DPC

The results are obtained at a wind speed of 12 m/sec. The trapezoidal wave form shown in Figure 7 shows the pattern of step change in the reactive reference which is applied to both the control techniques. The trapezoidal pattern wasselected to examine the system behavior following variation in the wind speed with both negative and positive slopes. The selectedwind speed pattern spans an input mechanical wind powerfrom 0.7 to 1 p.u. (70 to 100% of the turbine-generator ratedpower).

Figures 8(a) and 8(b) show the Real and Reactive power tracking of DFIG against disturbances present in the given wind speed pattern. Because of coupling of all powers interlinked to each other, the coupling effect is obtained at t=0.3 sec.

Figure 9(a) shows the Real power tracking of DFIG against disturbances in the given wind speed pattern. Here the dip in the wave form shows the start of real power generation at t=0.2 sec. Figure 9(b) indicates the reactive power absorption for 0.4 sec.

Figures 10(a) and 10(b) show the dc link voltages of Power transfer matrix control and DPC. The change in wind speed leads to the fluctuations of the dc link voltage. Due to the coupling of all powers  $v_{dc}$  of power transfer matrix have some variations. Where as in DPC there is no coupling of the powers and the dc link voltage is constant. Change in wind speed does not affect dc link voltage

## 7. CONCLUSION

Upon examining the results of both Power transfer matrix and DPC techniques for the same disturbances the Real power generation is better in power transfer matrix control than with DPC. Also the generation of power starts in DPC with a delay of 0.2 sec. Hence power transfer matrix method is giving better results than the DPC method.

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