# FOC of SRM using More Efficient DC-DC Converter Topology 

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#### Abstract

Numerous studies had been made to improve the switched reluctance motor operation depend on the modification of the machine design, proposing the converter designs and/or applying a suitable control method. This paper introduces the field orientation control method for that motor using a simple and very efficient DC-DC converter topology. This control method is presented by two techniques; first technique is the advance of the turn-on switching angle and the other technique is the retard/delay of the turn-off switching angle. Instantaneous and average motor characteristics are obtained using Matlab/Simulink software package. Comparison between the simulation results presented using two converter types. A precise speed and torque control are obtained. The average total torque per current is maximized.


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## 1. INTRODUCTION

The switched reluctance motor (SRM) is being used in various number of applications because of it has many merits over the other motor types. The SRM has a simple and robust construction. However, it basically generates large torque ripples compared with the other types of brushless DC motors. For that reason, to improve its operation and reducing the torque ripples, a development in its converter construction and/or a best control strategy is used [1]-[6], [37]-[38].

One of the main approaches of the research in SRM drives is the converter design. The operation and the cost of SRM drive system is mainly affected by the performance of the motor converter [7,8]. Many converter topologies have emerged through continued researches by reducing the number of switches in the converter and also getting faster switch commutation time [3,9-10]. This leads to a simple drive system and enables significant energy savings [11]-[14]. A high performance SRM drive is mainly characterized by minimization of the torque ripples and maximization of the motor efficiency and the torque per current [6],[15]. This criterion can be realized by optimizing the control parameters of the motor such as supply voltage, current level, turn-on, turn-off and the dwell angle [16]-[20].

A closed loop control with a simple DC-DC converter construction [21] for a 3-phase 6/4 SRM with Field Orientation Control (FOC) (known as some times; the switching angle control) method is introduced in this research to get the most efficient operation over the entire range operation of the SRM.

The complete block control diagram for a 3-ph 6/4 SRM drive system using FOC is shown in Figure 1. A standard DC source of 220 V is used with the $3-\mathrm{ph}$ DC-DC converter. The speed sensor is an integral part of the SRM drive system, may be optical encoders, resolver or hall-effect sensor [22]-[24] is mounted on the motor shaft to determine the actual rotor speed. A speed-angle converter can used to convert the measured speed into actual measured angle $\left(\theta_{m}\right)$ for comparison with the turn-on $\left(\theta_{o n}\right)$ angle and the turnoff ( $\theta_{\text {off }}$ ) angle to excite and commutate the phase windings. A digital controller named as a switching angle
controller [25] is used to synchronize the switching angles with their respective positions. This angle controller regulates the angles at which excitation of motor phases is achieved. So, it allows the rotor to continuously rotate, producing torque in accordance with the load being applied. The gate drive circuit (triggering circuit) contains integrated circuit components must be used between the angle controller and the power converter. The control logic signals are too small to drive the power switches of the converter. So, the gate drive circuit is used to amplify the control logic signals to the value of current levels required for switching the power converter, and also acts as a good isolation circuit (because it contains opto-coupler) between controller circuit and converter [26].


Figure 1. Main components of SRM drive system

This research is organized as follows. The operation of SRM and its mathematical model are reviewed in Section 2. DC-DC converter topology is presented in Section 3. Simulation results using FOC are illustrated in Section 4. The research conclusions are given in Section 5.

## 2. OPERATION AND MATHEMATICAL MODEL OF SRM

Due to the advances in power electronics, sensors and controllers in the recent years, the SRM has gained a great of commercial and industrial interest [27]. It has a simple and robust construction due to the magnetic circuitry of the motor neither requires permanent magnets nor windings in the rotor. The stator has concentrated coils around the poles that are excited sequentially through DC voltage pulses. The motor has salient poles on the stator and also on the rotor, so, it is named as a doubly salient pole machine [27,28]. The term "switched reluctance" tends to that the reluctance of the machine is switched. The term magnetic "reluctance" depends on the rotor position and the term "switched" refers to the electronic commutation of the electrical phases by means of a power electronics converter [28].


Figure 2. Unaligned and aligned positions for phase-A of a 3-phase 6/4 SRM
The SRM torque production is based purely on the variation of the magnetic reluctance. The magnetic circuits of the motor are symmetrical and have almost zero mutual flux linkages among stator
windings even under saturated conditions. The self inductance of the phase windings only is responsible for production of torque [28]. Figure 2 shows a typical three-phase machine configuration, $N_{p h}=3$. The machine has six stator poles $N_{s}=6$ and four rotor poles $N_{R}=4$, this configuration is known as a $6 / 4 \mathrm{SRM}$. From a magnetic perspective, each phase of the $6 / 4$ machine has two magnetic poles per phase, i.e., one pole pair, given that diametrically opposed coils are electrically connected in series or in parallel. For example, the phase A is made up of concentrated coils on poles A and A'. The rotor position shown in Figure 2a is called the unaligned position with respect to phase $\mathrm{A}-\mathrm{A}^{\prime}$, this unaligned position for the phase A is the position of the largest magnetic reluctnace between stator and rotor poles. If the phase A is excited, a magnetic flux path is formed by the two stator pole $\mathrm{A}-\mathrm{A}^{\prime}$, as in Figure 2b, which is the position of the smallest magnetic reluctance [29]. The complete mathematical model of the SRM in [21] is a set of differential equations which are obtained using standard electromagnetic theory. These differential equations are as follows:

$$
\begin{equation*}
U_{j}=i_{j} R_{j}+\frac{d \lambda_{j}\left(i_{j}, \theta\right)}{d \theta} \tag{1}
\end{equation*}
$$

Where $U_{j}$ denotes the phase voltage, $i_{j}$ denotes the phase current, $R_{j}$ denotes the phase resistance, $j$ is the active phase, and $\lambda_{j}\left(i_{j}, \theta\right)$ is the flux linkage. Equation (1) can be rewritten as:

$$
\begin{equation*}
U_{j}=i_{j} R_{j}+\frac{\partial \lambda_{j}\left(i_{j}, \theta\right)}{\partial i} \frac{d i_{j}}{d t}+\frac{\partial \lambda_{j}\left(i_{j}, \theta\right)}{\partial \theta} \frac{d \theta}{d t} \tag{2}
\end{equation*}
$$

The flux linkage in an active phase is given by the product of the self-inductance and the instantaneous phase current as follows:

$$
\begin{equation*}
\lambda_{j}\left(i_{j}, \theta\right)=L_{j}\left(i_{j}, \theta\right) \cdot i_{j} \tag{3}
\end{equation*}
$$

By substituting from Equation (3) into Equation (2) gives:

$$
\begin{align*}
& U_{j}=i_{j} R_{j}+L_{j i n c} \cdot \frac{d i_{j}}{d t}+i_{j} \cdot \frac{\partial L_{j}\left(i_{j}, \theta\right)}{\partial \theta} \cdot \omega  \tag{4}\\
&=i_{j} R_{j}+L_{j i n c} \cdot \frac{d i_{j}}{d t}+K_{v} \cdot \omega  \tag{5}\\
& L_{\text {jinc }}=\frac{\partial \lambda_{j}\left(i_{j}, \theta\right)}{\partial i}=\frac{\partial L_{j}\left(i_{j}, \theta\right) \cdot i_{j}}{\partial i}=L_{j}\left(i_{j}, \theta\right)+i_{j} \cdot \frac{\partial L_{j}\left(i_{j}, \theta\right)}{\partial i}  \tag{6}\\
& \omega=\frac{d \theta}{d t} \tag{7}
\end{align*}
$$

Where $L_{j i n c}$ is the phase incremental inductance, $K_{v}$ is the current-dependent back-emf coefficient, and $\omega$ is the rotor angular speed. Rearranging Equation (4) gives:

$$
\begin{align*}
& \frac{d i_{j}}{d t}=\frac{1}{L_{j i n c}}\left(U_{j}-i_{j} R_{j}-i_{j} \cdot \frac{\partial L_{j}\left(i_{j}, \theta\right)}{\partial \theta} \cdot \omega\right)  \tag{8}\\
& J \frac{d^{2} \theta}{d t^{2}}=J \frac{d \omega}{d t}=\sum_{J=1}^{K} T_{j}\left(i_{j}, \theta\right)-B \omega-T_{L}(\omega) \tag{9}
\end{align*}
$$

Where $J$ and $B$ are the moment of inertia and the viscous friction coefficient, respectively; and $T_{L}$ is the load torque. Equations (7), (8) and (9) represent the complete mathematical model of the SRM in the case of nonlinear modeling for operation of the motor in a real mode. With the non-linear operation; the shape of the inductance is sinusoidal depends on the rotor position, the phase current, and the motor geometry.

The static SRM characteristics can be represented basically via two methods. The first is to plot the variation of phase inductance with respect to rotor position at different phase currents; this way is used in this research. The second way is to plot the variation of phase flux linkage with rotor position and phase currents.

## 3. DC-DC CONVERTER TOPOLOGY

The SRM cannot run directly from AC or DC source; unlike induction motors or DC motors. So, a power electronics DC-DC converter must be located between the motor and the source. The purpose of the power converter circuit is to provide an increasing and decreasing the current supplied to the phase winding in order to produce a continuous motion [28]. In the feedback path between the motor and the power converter, a control circuit is used to monitor the current and the position feedback in order to produce the correct switching signals for the power converter for matching the demands placed on the drive by the user.

Since the torque developed by the SRM not depends on the current polarity, the motor can operate based on the principle of unipolar current. The current therefore can be supplied to the phase winding with only one switch per phase connected in series with the winding, as shown in Figure 3 [21]. By turning on and off this switch; the flow of the phases current can be regulated. The best feature for that converter is that each phase contains only one switch. This converter topology can be used with a three phases SRM and can be simply modified to suit another type of SRM has different number of phases. Since the mutual coupling between phases is almost negligible, the stored magnetic field energy can create problem during commutation of the phase. The stored magnetic field energy has to be provided a path during commutation (as shown in Figure 3, a freewheeling diode is used in each phase): otherwise excessive voltage can develop across the winding and may result in failure of the semiconductor switch that connected in series with the phase winding [30]-[32].


Figure 3. Simple DC-DC converter for 3-phase, 6/4 SRM

As shown in Figure 3, the power switches can be protected using RC snubber circuit. This snubber circuit protects the switch from a large $d i / d t$ during turn-on and large $d v / d t$ during turn-off. Also the snubber circuit provides an effective means of transferring the switching losses from the switch to the snubber resistor, leading to a lower junction temperature rise and better thermal management for the switch and also the no recover of energy to DC source not cause reduction of the overall efficiency of the drive drive [33]-[34].

The diode $D_{s}$ is used to safe the DC source from the recover energy of each motor phase. No reduction of the overall efficiency of the motor drive because there is no recover of energy to the DC source. The steady state of motor characteristics is reaches faster than using the traditional DC-DC converters [35]-[36].

## 4. SIMULATION RESULTS USING FOC

The torque of SRM has a strong pulsations at the commutation intervals because the two adjacent phases produce additive torques. Therefore, the FOC can be used to control the SRM drive. This control strategy is based on controlling the values of the switching angles and the dwell angle. The machine efficiency and the average total torque per current will maximize by using this control strategy. So, the FOC
is used to control the dwell angle and the input source voltage instantaneously in order to obtain a precise speed control.

In the real control system, control of the switching angles can be realized by a simple feedback circuit using detecting position sensor on the motor shaft as shown in Figure 4. The switching angle controller in that figure regulates the motor performance via integration of the motor speed to produce the measured position of the rotor by comparing the measured rotor position with the switching angles $\theta_{\text {on }}$ and $\theta_{\text {off. }}$ In order to produce the gate signals of the converter switches. A gate drive circuit must be used between the angle controller and the converter, it receives the logic signals that has a low level from the angle controller and transmit these signals but with a high level to the converter. In other means; the gate drive circuit is used to isolate the control circuit from the power circuit.


Figure 4. Complete block control diagram for 3-ph 6/4 SRM drive system using Field Orientation Control

The back-emf in the motor becomes significant as the motor speed increases. It is necessary to retard the turn-off angle or advance the turn-on angle in order to reach the reference current before the poles overlap. One reason of the torque ripple is that the negative torque due to the tail current (which will be solved using the FOC method). Also, the decay of current in the demagnetizing case can be enhanced through decaying it in fast time using FOC. In this part, the motor firing/switching angles change by the means of a software to obtain the best values for these angles.

The block control diagram of Figure 4 can be simulated using Matlab/Simulink software package. The data required for that motor drive system obtained from the APPENDIX. The simulation results obtained for no-load, $\theta_{\text {on }}=40^{\circ}$, and $\theta_{\text {off }}=70^{\circ}$.

### 4.1. Instantaneous Characteristics with Advance Turn-On

The instantaneous phase current versus rotor position is shown in Figure 5. The principle of increasing the advance of the turn-on angle $\theta_{\text {on }}$ (i.e., decreasing the value of the turn-on angle) is to increase the average motor total torque. The phase current $I_{A}$ has $\theta_{\text {on }}=40^{\circ}, \theta_{\text {off }}=70^{\circ}$ and advance for $\theta_{\text {on }}$ by a step of $2^{\circ}$. The phase current $I_{A}$ has three cases for advance of $\theta_{o n}$. The case of the solid line (where, $\theta_{o n}=40^{\circ}$ ) there is no advance for the phase current. The case of the dashed line (where, $\theta_{\text {on }}=38^{\circ}$ ) an advance by $2^{\circ}$ is obtained. The case of the dotted line (where, $\theta_{\text {on }}=36^{\circ}$ ), the phase current has an advance by $4^{\circ}$. Then, when we see deeply, the phases current increases as the turn-on angle is advanced, also, the motor total current or the source current increases (but this is undesirable) to produce an increase in the average total torque as shown in Figure 5 and Figure 6 respectively.


Figure 5. Instantaneous motor phases current versus rotor position for advance turn-on

As shown in Figure 5 the phase current increases with increasing the advance turn-on, because the conduction period of the phase current increases as the advance increases. But, there is a limit of increasing the phase current to be not greater than a maximum allowable range. This maximum allowable current occurs when the source current has the value 1.25 of the rated source current. For that converter design; the average steady state phase current at $\theta_{\text {on }}=40^{\circ}, \theta_{\text {off }}=70^{\circ}$ equals to 0.42 A , but for the asymmetric bridge at the same switching angles, the average steady state phase current equals 0.9 A [35].


Figure 6. Instantaneous source current versus rotor position for advance turn-on

The instantaneous total torque versus rotor position is shown in Figure 7 the total torque increases as the advance of the turn-on angle increases, also, if there is a negative torque found, the advance can eliminate it. The average total torque at $\theta_{\text {on }}=40^{\circ}$ and $\theta_{\text {off }}=70^{\circ}$ equals 4.279 Nm but in the asymmetric bridge converter equals 2.160 Nm [35].


Figure 7. Instantaneous motor total torque versus rotor position for advance turn-on

### 4.2. Instantaneous Characteristics with Retard Turn-Off

On the other hand, the principle of retarding the turn-off angle (i.e., increasing the value of the turn-off angle $\theta_{\text {off }}$ ) based on increasing the conduction period between the switching angles for increasing the average motor total torque. The instantaneous phase's current versus rotor position for retard the turn-off is shown in Figure 8. The phase current $I_{A}$ has constant angles $\theta_{\text {on }}=40^{\circ}, \theta_{\text {off }}=70^{\circ}$ and retard for $\theta_{\text {off }}$ by step of $2^{\circ}$. The phase current $I_{A}$ has three cases for retad/delay of $\theta_{o f f}$. The case of solid line there is no delay (where, $\theta_{\text {off }}=70^{\circ}$ ). The case of the dashed line a delay by $2^{\circ}$ (where $\theta_{\text {off }}=72^{\circ}$ ) is obtained. The case of the dotted line (where, $\theta_{\text {off }}=74^{\circ}$ ) the phase current has a delay by $4^{\circ}$. Then, when we see deeply, the phases current decreases as the turn-off angle is delayed further, also, the motor total current decreases (this is desirable); but the motor total torque decreases as the retarding/delaying of the turn-off angle increases, as shown in Figure 9 and Figure 10 respectively.


Figure 8. Instantaneous motor phases current versus rotor position for retard turn-off

As shown in Figure 7 and Figure 10; the motor total torque at using the retarding of the turn-off angle has a less negative vaule compared with using advancing of the turn-on angle. Also as shown in Figure 5 and Figure 8; the average value of motor phase current increases as the advance turn-on increases but decreases as the retard of the turn-off increases. Similarly, as presented in Figure 6 and Figure 9 the
instantenous source current increases as advance turn-on increases, but decreases as the retard turn-off increases.


Figure 9. Instantaneous source current versus rotor position for retard turn-off


Figure 10. Instantaneous motor total torque versus rotor position for retard turn-off

### 4.3. Average Characteristics with Advance Turn-On

For easy comparison between motor characteristics at using the advance turn-on and the retard turn-off; the motor average characteristics are introduced. The average source current versus rotor position at using advance turn-on, is shown in Figure 11; at constant the turn-off angle (say $\theta_{o f f}=70^{\circ}$ ), as the switching turn-on angle decreases the average source current increases. Also; as shown in Figure 12; at constant turnoff angle (say, $\theta_{\text {off }}=70^{\circ}$ ) as the switching turn-on angle decreases, the average total torque increases. In other words, for constant turn-off angle; the average source current or average total torque increases as the advance of the turn-on angle increases.

From Figure 11 and Figure 12; more advancing of turn-on angle produces large increase in the average source current and a small increase in the average total torque, so, this will lead to decrease in the average total torque per current as presented in Figure 13. Also, as shown in Figure 14, increasing the advance of turn-on angle leads to increases of motor speed.


Figure 11. Average source current versus rotor position for advance turn-on


Figure 12. Average total torque versus rotor position for advance turn-on


Figure 13. Average total torque per current versus rotor position for advance turn-on


Figure 14. Motor speed versus rotor position for advance turn-on

### 4.4. Average Characteristics with Retard Turn-Off

After presentation of average characteristics with the change of the rotor position at using advance turn-on angle; the average characteristics for the retard turn-off is presented in this subsection. As shown in Figure 15 for a constant turn-on angle (say, $\theta_{o n}=40^{\circ}$ ), as the value of the turn-off angle increases, the average source current increases. This means that, the average source current increases as the retard of the turn-off angle increases. Similarly, as shown in Figure 16, the average total torque increases as the retard of the turn-off angle increases.


Figure 15. Average source current versus rotor position for retard turn-off

As shown in Figure 17 the average total torque per current versus rotor position is presented at using a constant turn-on angle and applying variation for the turn-off angle. The torque per current increases from $\theta_{\text {off }}=64^{\circ}$ until $68^{\circ}$ and decreases from $\theta_{\text {off }}=70^{\circ}$ until $74^{\circ}$. But this is not standard case for variation of the turn-off angle. Also, as shown in Figure 18 increase the retarding of the turn-off angle, this leads to an increase in the motor speed.

In order to the motor phases respond to continuous drawing of a current from the source, there is a maximum allowable range of $\theta_{\text {on }}$ and $\theta_{\text {off }}$ for $3-\mathrm{ph} 6 / 4$ SRM. The motor average characteristics values for this range will be stored in the following tables. These characteristics obtained at steady state speed by applying a rated source voltage of 220 V .


Figure 16. Average total torque versus rotor position for retard turn-off


Figure 17. Average total torque per ampere versus rotor position for retard turn-off


Figure 18. Motor speed versus rotor position for retard turn-off

The average source current is shown in Table 1 at different values of turn-on and turn-off angles to obtain the optimum performance $\mathrm{ch} / \mathrm{s}$ for the drive system at no-load; where the minimum allowable limit and the maximum allowable limit of the switching angles are presented. From Table 1 adjustment of the switching angles (turn-on angle of $60^{\circ}$ and turn-off angle of $64^{\circ}$ ) is presented in order to get a minimum average source current of 0.107 A (at using the asymmetric bridge converter equals 0.152 A ) [36]. But in Table 2 the maximum average total torque is 4.552 Nm at turn-on angle of $36^{\circ}$ and turn-off angle of $80^{\circ}$ (at using the asymmetric bridge converter equals 2.224 Nm ) [36]. But this value of the torque not present optimum machine performance because the optimum performance depends on the maximum torque per current is $6.016 \mathrm{Nm} / \mathrm{A}$ at turn-on angle of $60^{\circ}$ and turn-off angle of $68^{\circ}$ (at using the asymmetric bridge converter equals 2.224 Nm ) [36] as presented in Table 3. The motor speed at all switching angles is presented in Table 4.

Table 1. The Average source current of proposed converter in (Ampere)

| $\theta_{\text {off }}$ | $64^{\circ}$ | $66^{\circ}$ | $68^{\circ}$ | $70^{\circ}$ | $72^{\circ}$ | $74^{\circ}$ | $76^{\circ}$ | $78^{\circ}$ | $80^{\circ}$ | $82^{\circ}$ | $84^{\circ}$ | $86^{\circ}$ | $88^{\circ}$ | $90^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta_{\text {on }}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $36^{\circ}$ | 1.090 | 1.120 | 1.156 | 1.199 | 1.247 | 1.301 | 1.361 | 1.428 | 1.501 | 1.582 | 1.672 | 1.773 | 1.885 | 2.013 |
| $38^{\circ}$ | 0.970 | 1.002 | 1.039 | 1.081 | 1.128 | 1.181 | 1.238 | 1.302 | 1.373 | 1.451 | 1.537 | 1.633 | 1.742 | 1.865 |
| $40^{\circ}$ | 0.857 | 0.891 | 0.929 | 0.971 | 1.017 | 1.067 | 1.124 | 1.187 | 1.255 | 1.330 | 1.413 | 1.507 | 1.613 | 1.733 |
| $42^{\circ}$ | 0.753 | 0.787 | 0.826 | 0.868 | 0.914 | 0.964 | 1.019 | 1.080 | 1.146 | 1.220 | 1.301 | 1.393 | 1.496 | 1.615 |
| $44^{\circ}$ | 0.656 | 0.692 | 0.730 | 0.773 | 0.818 | 0.868 | 0.922 | 0.981 | 1.046 | 1.118 | 1.198 | 1.288 | 1.390 | 1.508 |
| $46^{\circ}$ | 0.566 | 0.603 | 0.643 | 0.684 | 0.730 | 0.779 | 0.832 | 0.890 | 0.954 | 1.025 | 1.104 | 1.193 | 1.294 | 1.411 |
| $48^{\circ}$ | 0.485 | 0.522 | 0.562 | 0.603 | 0.648 | 0.696 | 0.748 | 0.806 | 0.869 | 0.939 | 1.016 | 1.105 | 1.205 | 1.322 |
| $50^{\circ}$ | 0.409 | 0.448 | 0.487 | 0.529 | 0.573 | 0.620 | 0.672 | 0.729 | 0.790 | 0.859 | 0.936 | 1.023 | 1.123 | 1.240 |
| $52^{\circ}$ | 0.339 | 0.379 | 0.419 | 0.460 | 0.504 | 0.550 | 0.600 | 0.656 | 0.717 | 0.785 | 0.861 | 0.948 | 1.048 | 1.165 |
| $54^{\circ}$ | 0.276 | 0.316 | 0.356 | 0.397 | 0.440 | 0.485 | 0.535 | 0.589 | 0.650 | 0.716 | 0.791 | 0.877 | 0.977 | 1.095 |
| $56^{\circ}$ | 0.216 | 0.257 | 0.297 | 0.338 | 0.380 | 0.424 | 0.474 | 0.527 | 0.586 | 0.652 | 0.726 | 0.811 | 0.911 | 1.030 |
| $58^{\circ}$ | 0.160 | 0.201 | 0.243 | 0.283 | 0.323 | 0.368 | 0.416 | 0.469 | 0.526 | 0.591 | 0.664 | 0.748 | 0.848 | 0.968 |
| $60^{\circ}$ | 0.107 | 0.149 | 0.191 | 0.231 | 0.272 | 0.315 | 0.362 | 0.413 | 0.469 | 0.534 | 0.605 | 0.689 | 0.789 | 0.910 |

Table 2. The Average total torque of proposed converter in (Newton.meter)

| $\theta_{\text {off }}$ | $64^{\circ}$ | $66^{\circ}$ | $68^{\circ}$ | $70^{\circ}$ | $72^{\circ}$ | $74^{\circ}$ | $76^{\circ}$ | $78^{\circ}$ | $80^{\circ}$ | $82^{\circ}$ | $84^{\circ}$ | $86^{\circ}$ | $88^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta_{\text {on }}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $36^{\circ}$ | 3.608 | 3.845 | 4.042 | 4.202 | 4.328 | 4.424 | 4.492 | 4.534 | 4.552 | 4.545 | 4.517 | 4.465 | 4.392 |
| $38^{\circ}$ | 3.457 | 3.693 | 3.889 | 4.049 | 4.177 | 4.275 | 4.344 | 4.387 | 4.406 | 4.401 | 4.373 | 4.323 | 4.250 |
| $40^{\circ}$ | 3.283 | 3.518 | 3.716 | 3.878 | 4.008 | 4.109 | 4.181 | 4.226 | 4.247 | 4.244 | 4.218 | 4.169 | 4.098 |
| $42^{\circ}$ | 3.084 | 3.321 | 3.521 | 3.687 | 3.821 | 3.925 | 4.000 | 4.049 | 4.073 | 4.073 | 4.049 | 4.003 | 3.933 |
| $44^{\circ}$ | 2.862 | 3.101 | 3.305 | 3.476 | 3.615 | 3.724 | 3.804 | 3.857 | 3.885 | 3.888 | 3.868 | 3.824 | 3.757 |
| $46^{\circ}$ | 2.617 | 2.860 | 3.070 | 3.247 | 3.392 | 3.506 | 3.592 | 3.651 | 3.684 | 3.692 | 3.676 | 3.635 | 3.571 |
| $48^{\circ}$ | 2.355 | 2.603 | 2.819 | 3.003 | 3.156 | 3.277 | 3.369 | 3.434 | 3.473 | 3.485 | 3.473 | 3.437 | 3.376 |
| $50^{\circ}$ | 2.080 | 2.333 | 2.555 | 2.748 | 2.908 | 3.037 | 3.138 | 3.209 | 3.253 | 3.272 | 3.265 | 3.231 | 3.174 |
| $52^{\circ}$ | 1.792 | 2.050 | 2.284 | 2.484 | 2.652 | 2.791 | 2.899 | 2.978 | 3.029 | 3.053 | 3.051 | 3.024 | 2.969 |
| $54^{\circ}$ | 1.500 | 1.763 | 2.002 | 2.212 | 2.393 | 2.540 | 2.657 | 2.744 | 2.803 | 2.834 | 2.838 | 2.814 | 2.764 |
| $56^{\circ}$ | 1.204 | 1.475 | 1.720 | 1.940 | 2.127 | 2.287 | 2.413 | 2.509 | 2.576 | 2.613 | 2.624 | 2.606 | 2.560 |
| $58^{\circ}$ | 0.909 | 1.182 | 1.435 | 1.661 | 1.862 | 2.031 | 2.168 | 2.273 | 2.350 | 2.395 | 2.412 | 2.400 | 2.359 |
| $60^{\circ}$ | 0.613 | 0.889 | 1.151 | 1.385 | 1.596 | 1.775 | 1.923 | 2.039 | 2.124 | 2.177 | 2.202 | 2.198 | 2.162 |

Table 3. The Average total torque per mpere of proposed converter in (Newton.meter/Ampere)

| $\theta_{\text {off }}$ | $64^{\circ}$ | $66^{\circ}$ | $68^{\circ}$ | $70^{\circ}$ | $72^{\circ}$ | $74^{\circ}$ | $76^{\circ}$ | $78^{\circ}$ | $80^{\circ}$ | $82^{\circ}$ | $84^{\circ}$ | $86^{\circ}$ | $88^{\circ}$ | $90^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta_{\text {on }}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $36^{\circ}$ | 3.309 | 3.432 | 3.494 | 3.504 | 3.470 | 3.400 | 3.300 | 3.176 | 3.032 | 2.873 | 2.700 | 2.519 | 2.330 | 2.135 |
| $38^{\circ}$ | 3.564 | 3.687 | 3.744 | 3.746 | 3.703 | 3.621 | 3.508 | 3.369 | 3.210 | 3.035 | 2.846 | 2.647 | 2.440 | 2.228 |
| $40^{\circ}$ | 3.829 | 3.949 | 4.002 | 3.996 | 3.940 | 3.849 | 3.720 | 3.561 | 3.385 | 3.191 | 2.984 | 2.766 | 2.541 | 2.310 |
| $42^{\circ}$ | 4.100 | 4.217 | 4.264 | 4.248 | 4.181 | 4.070 | 3.926 | 3.750 | 3.553 | 3.339 | 3.112 | 2.874 | 2.629 | 2.379 |
| $44^{\circ}$ | 4.366 | 4.484 | 4.525 | 4.499 | 4.418 | 4.290 | 4.127 | 3.931 | 3.713 | 3.477 | 3.228 | 2.969 | 2.702 | 2.433 |
| $46^{\circ}$ | 4.624 | 4.742 | 4.778 | 4.745 | 4.649 | 4.503 | 4.321 | 4.102 | 3.862 | 3.603 | 3.330 | 3.048 | 2.760 | 2.469 |
| $48^{\circ}$ | 4.863 | 4.985 | 5.021 | 4.977 | 4.868 | 4.706 | 4.503 | 4.261 | 3.997 | 3.713 | 3.418 | 3.111 | 2.801 | 2.489 |
| $50^{\circ}$ | 5.082 | 5.209 | 5.246 | 5.196 | 5.075 | 4.895 | 4.672 | 4.407 | 4.118 | 3.810 | 3.488 | 3.158 | 2.825 | 2.492 |
| $52^{\circ}$ | 5.274 | 5.411 | 5.452 | 5.398 | 5.267 | 5.070 | 4.827 | 4.538 | 4.225 | 3.891 | 3.545 | 3.191 | 2.834 | 2.480 |
| $54^{\circ}$ | 5.447 | 5.587 | 5.632 | 5.580 | 5.442 | 5.232 | 4.968 | 4.656 | 4.318 | 3.958 | 3.586 | 3.208 | 2.829 | 2.453 |
| $56^{\circ}$ | 5.580 | 5.760 | 5.788 | 5.743 | 5.599 | 5.390 | 5.095 | 4.759 | 4.396 | 4.011 | 3.615 | 3.211 | 2.809 | 2.414 |
| $58^{\circ}$ | 5.680 | 5.884 | 5.920 | 5.877 | 5.754 | 5.518 | 5.208 | 4.851 | 4.472 | 4.053 | 3.635 | 3.207 | 2.781 | 2.364 |
| $60^{\circ}$ | 5.717 | 5.973 | 6.016 | 5.987 | 5.868 | 5.631 | 5.314 | 4.935 | 4.525 | 4.081 | 3.640 | 3.187 | 2.739 | 2.303 |

Table 4. The Average motor speed of proposed converter in (revolution per minute)

| $\theta_{\text {off }}$ | $64^{\circ}$ | $66^{\circ}$ | $68^{\circ}$ | $70^{\circ}$ | $72^{\circ}$ | $74^{\circ}$ | $76^{\circ}$ | $78^{\circ}$ | $80^{\circ}$ | $82^{\circ}$ | $84^{\circ}$ | $86^{\circ}$ | $88^{\circ}$ | $90^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta_{\text {on }}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $36^{\circ}$ | 1883 | 2006 | 2109 | 2192 | 2259 | 2309 | 2344 | 2366 | 2375 | 2372 | 2357 | 2330 | 2292 | 2242 |
| $38^{\circ}$ | 1804 | 1927 | 2029 | 2113 | 2180 | 2231 | 2267 | 2289 | 2299 | 2297 | 2282 | 2256 | 2218 | 2168 |
| $40^{\circ}$ | 1713 | 1836 | 1939 | 2024 | 2091 | 2144 | 2181 | 2205 | 2216 | 2215 | 2201 | 2175 | 2138 | 2089 |
| $42^{\circ}$ | 1609 | 1733 | 1837 | 1924 | 1994 | 2048 | 2087 | 2113 | 2125 | 2125 | 2113 | 2089 | 2053 | 2004 |
| $44^{\circ}$ | 1493 | 1618 | 1725 | 1814 | 1886 | 1943 | 1985 | 2013 | 2027 | 2029 | 2018 | 1996 | 1961 | 1914 |
| $46^{\circ}$ | 1366 | 1492 | 1602 | 1694 | 1770 | 1830 | 1875 | 1905 | 1922 | 1927 | 1918 | 1897 | 1863 | 1817 |
| $48^{\circ}$ | 1229 | 1358 | 1471 | 1567 | 1647 | 1710 | 1758 | 1792 | 1812 | 1819 | 1812 | 1793 | 1761 | 1716 |
| $50^{\circ}$ | 1085 | 1217 | 1334 | 1434 | 1518 | 1585 | 1637 | 1675 | 1698 | 1707 | 1703 | 1686 | 1656 | 1613 |
| $52^{\circ}$ | 936 | 1070 | 1191 | 1296 | 1384 | 1456 | 1513 | 1554 | 1581 | 1593 | 1592 | 1578 | 1549 | 1507 |
| $54^{\circ}$ | 783 | 921 | 1045 | 1155 | 1248 | 1325 | 1386 | 1432 | 1462 | 1479 | 1481 | 1468 | 1442 | 1402 |
| $56^{\circ}$ | 629 | 769 | 897 | 1012 | 1110 | 1193 | 1259 | 1309 | 1344 | 1364 | 1369 | 1360 | 1336 | 1297 |
| $58^{\circ}$ | 474 | 617 | 748 | 867 | 972 | 1060 | 1131 | 1186 | 1226 | 1250 | 1259 | 1253 | 1231 | 1194 |
| $60^{\circ}$ | 320 | 465 | 600 | 723 | 832 | 926 | 1003 | 1064 | 1108 | 1137 | 1149 | 1147 | 1128 | 1093 |

## 5. CONCLUSIONS

At steady state; for a constant value of $\theta_{o f f}$; if the advancing of $\theta_{o n}$ increases (i.e, decreasing the value of $\theta_{o n}$ ), then: the average source current, average total torque and motor speed are directly proportional to advance of the $\theta_{\text {on }}$. The average total torque per current is inversely proportional to advance of the $\theta_{\text {on }}$. At steady state; for a constant value of $\theta_{o n}$; if the retarding/delaying of $\theta_{o f f}$ increases (i.e, increasing value of $\theta_{o f f}$, then: the average source current, average total torque and motor speed are directly proportional to retard of $\theta_{o f f}$. The average total torque per current is inversely proportional to retard of $\theta_{o f f}$. At steady state, for a constant switching angles: the average source current is inversely proportional to increase of source voltage. The average total torque, average total torque per current and the motor speed are directly proportional to increase of source voltage.

## APPENDIX

| DC voltage rating | $: U$ | $=220 \mathrm{~V}$ |
| :--- | :--- | :--- |
| Stator phase resistance | $: R$ | $=17 \Omega$ |
| Aligned inductance | $: L_{a l}$ | $=0.605 \mathrm{H}$ |
| Unaligned inductance | $: L_{u l}$ | $=0.155 \mathrm{H}$ |
| Viscous friction coefficient | $: B$ | $=0.0183 \mathrm{~N} \cdot \mathrm{~m} \cdot \mathrm{Sec}^{2}$ |
| Rated speed | $: n_{r}$ | $=1000 \mathrm{rpm}$ |
| Rated phase current | $: I_{r}$ | $=3 \mathrm{~A}$ |
| Rated torque | $: T_{e}$ | $=1 \mathrm{Nm}$ |
| Inertia constant | $: J$ | $=0.0013 \mathrm{Kg} \cdot \mathrm{m}^{2}$ |

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