An application for nonlinear control by input-output linearization technique for pm synchronous motor drive for electric vehicles

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ABSTRACT
This paper leads to present the modified approach of the speed control for permanent magnet synchronous motors applied to electric vehicles using a nonlinear control. The motor's nonlinear dynamics are transformed into a linearized system model using the input-output feedback linearization technique. There are two permanent magnet synchronous motors (PMSM) in the propulsion model. In order to improve the motor's output torque, the direct component of the current is adjusted to zero. The electronic differential, which is used in the calculations, enables each driving wheel to be controlled individually at each curve. The MATLAB/Simulink software is used to implement modeling and simulation in order to assess the effectiveness of the suggested solution. Simulation studies are used to confirm the efficacy of the proposed technique. The obtained results signify that this approach is more accurate.

Keywords:
Electric vehicle
Input-output feedback
Linearization
Nonlinear control
PMSM
Sliding mode control
Traction control

1. INTRODUCTION
With its high performance, permanent magnet synchronous motors (PMSM) has been hardlyexploited inquite high-performance drives such as machinetools and industrial robots. The fundamental drawback of PMSM, however, is the requirement for a complicated control unit that, because of its extremely non-linear properties, guarantees high-efficiency electric drive applications. The development of permanent magnet technology has led to the widespread use PMSM for various engineering applications, especially in variable-speed motors and electric vehicles were presented in [1], [2]. An efficient technique for controlling nonlinear systems is to linearize input-output feedback.

This section describes the nonlinear control strategy that was simply input output feedback control and depends on differential geometry techniques. The motor model can be split using these techniques into two separate monovariable linear subsystems. A perfect arrangement of the poles that reveals the dynamics of each subsystem was presented by Rebouh et al. [3].

The speed parameters of this controller are used within a drive system managessential objectives to reunite with other important criteria of the high-performance drive. Based on the literature, nonlinear systems have been traditionally developed by using classical linear control methods. These methods are only operational for a small operating range. In the case of a huge required operating range, the linear controller is

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no longer able to perform poorly. However, nonlinear controllers may operate the nonlinearities in range operations directly [4], [5].

Without a speed sensor, the research [6] described a direct torque control/sliding mode control DTC/SMC for IM training. The control method for an induction motor IM drive is built on the combination of SMC and stator flux field orientation control as presented in [6]. As an input-output feedback linearization technique, the vector control scheme's internal dynamics cannot be analytically shown to be stable under transient and steady state conditions. This means that unless the controller gains are properly set with more precision, the control system is only locally stable. In order to drive an induction motor without a sensor, The feedforward control principle, DTC, and modulation of spatial vectors (SVM) approach have been integrated and utilized in [7]. Because robust induction, a sort of field-oriented control, allows for extremely precise machine control, its development [8]–[15] marked a significant turning point in the field of electric drives.

The following describes how the paper is structured: The PMSM mathematical model is described in the second section. The third portion covers the whole design of control utilizing input-output linearization theory. Section 4 describes the parts of the electric traction system, whereas section 5 describes the parts of the electric differential system. Section 4 contains the simulation's results as well as a discussion of them. The last part explains the results obtained using the proposed controller.

2. PMSM MATHEMATICAL MODEL

According to the design in [12]–[18], PMSM drives the electric car's two rear wheels. More details based on the mathematical formulations can be found in the following section.

2.1. Description of machine equations

In this section, the mathematical representation of the PMSM in the rotor frame \((d-q)\) can be written as assuming that the PMSM is three-phase with balanced windings and no saturation [12].

\[
\begin{bmatrix}
v_a \\
v_q
\end{bmatrix} = \begin{bmatrix}
R_s + pL_d & -w_r L_q \\
w_r L_d & R_s + pL_q
\end{bmatrix} \begin{bmatrix}
i_a \\
i_q
\end{bmatrix} + \begin{bmatrix}
0 \\
w_r \varphi_f
\end{bmatrix}
\]

Applying the transformation of (1) from the \(d-q\) coordinate to \(\alpha-\beta\) coordinate, is given by (2) and (3).

\[
\begin{aligned}
v_a &= R_s i_a + w_r (L_d - L_q) i_\beta + E_a \\
v_\beta &= R_s i_\beta + L_d p i_\beta - w_r (L_d - L_q) i_a + E_\beta \\
F_a &= \left( \left( I_a - L_q \right) \left( w_r pi_a - pi_q \right) + w_r \varphi_f \right) (\sin \theta_r) \\
F_\beta &= \left( \left( I_a - L_q \right) \left( w_r pi_a - pi_q \right) + w_r \varphi_f \right) (\cos \theta_r)
\end{aligned}
\]

Where: \((v_a, v_\beta)\) and \((i_a, i_\beta)\) are the \((\alpha, \beta)\) axis voltage/current components, \(\varphi_r\) is Rotor angular.

Based on (2). In the following formula, the mathematical models for PMSM with fixed frames of reference \((\alpha, \beta)\) are presented by (4).

\[
\begin{bmatrix}
\frac{di_a}{dt} \\
\frac{di_\beta}{dt}
\end{bmatrix} = \begin{bmatrix}
\frac{-L_s}{L_d} & -w_r \left( \frac{L_d - L_q}{L_d} \right) \\
w_r \left( \frac{L_d - L_q}{L_d} \right) & \frac{-L_s}{L_d}
\end{bmatrix} \begin{bmatrix}
i_a \\
i_\beta
\end{bmatrix} + \begin{bmatrix}
- \frac{1}{L_d} & 0 \\
0 & \frac{1}{L_d}
\end{bmatrix} \begin{bmatrix}
E_a \\
E_\beta
\end{bmatrix} + \begin{bmatrix}
\frac{1}{L_d} (v_a) \\
\frac{1}{L_d} (v_\beta)
\end{bmatrix}
\]

The stator flux linkage and current expression for the electromagnetic torque \((T_e)\) of the PMSM as in (5).

\[
T_e = \frac{3}{2} p (\varphi_a i_\beta - \varphi_\beta i_a)
\]

The following represents the state flux linkage in the \(\alpha-\beta\) by (6).

\[
\begin{aligned}
\frac{d\varphi_a}{dt} &= v_a - R_s i_a \\
\frac{d\varphi_\beta}{dt} &= v_\beta - R_s i_\beta
\end{aligned}
\]

The stator flux linkage's amplitude \((\varphi_s)\) as in (7).
\[ \varphi_s = \sqrt{\varphi_a^2 + \varphi_b^2} \]  

(7)

The dynamic equation is delivered by (8).

\[ j \frac{dw_r}{dt} = p(T_e - T_L) - f w_r \]  

(8)

A dynamic model of the PM synchronous motors can be expressed using (2)-(8) as in (9).

\[
\begin{align*}
\frac{di_a}{dt} &= \left( -\frac{R_s}{L_d} i_a - \frac{R_s}{L_d} i_b \right) + \frac{1}{L_d} (e_a + \frac{k}{L_d} v_a) \\
\frac{di_b}{dt} &= \left( -\frac{1}{L_d} e_b + \frac{1}{L_d} v_a \right) + \frac{1}{L_d} (e_b + \frac{k}{L_d} v_b) \\
T_e &= \frac{2}{3} p \varphi_f (i_b \cos \theta_r - i_a \sin \theta_r) \\
\frac{dw_r}{dt} &= \frac{p}{J} (T_e - T_L) - \frac{f}{J} w_r
\end{align*}
\]  

(9)

3. ELECTRIC DRIVE SYSTEM COMPONENT MODELING

In this section, electric drive system component modeling is presented. Figure 1 depicts a general representation of an electric traction system that combined battery, inverter, PMSM, gears, and wheel. However, the PMSM speed controlled by electrical differential. This structure applied for two back wheels.

![Figure 1. The electric drive system's chain](image)

3.1. Description of energy source

In this section, a description of the energy source is provided. A lithium-ion battery system serves as the typical power source. Compared to other types of rechargeable batteries, lithium-ion battery innovation has benefits in the main aim of specific energy, specific power, and service life.

3.2. Model with inverters

In this example, the current battery in the electric traction system is provided to generate three balanced phases of variable frequency alternating current in [19].

\[
\begin{bmatrix}
V_a \\
V_b \\
V_c \\
\end{bmatrix} = \frac{v_{dc}}{3} \begin{bmatrix}
2 & -1 & -1 \\
-1 & 2 & -1 \\
-1 & -1 & 2 \\
\end{bmatrix} \begin{bmatrix}
S_a \\
S_b \\
S_c \\
\end{bmatrix}
\]  

(10)

3.3. Analysis of vehicle dynamics

The road load \( F_{\text{res}} \) the formula is based on the principles of vehicle dynamics and aerodynamics [5]–[10].
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\[ F_{rec} = F_{Rr} + F_{Sr} + F_{Ad} \]  \hspace{1cm} (11)

\( F_{Rr} \): rolling resistance, \( F_{Sr} \): slope resistance, \( F_{Ad} \): the aerodynamic drag.

\[ F_{Rr} = \mu Mg \]  \hspace{1cm} (12)

\[ F_{Sr} = Mg \sin(a) \]  \hspace{1cm} (13)

\[ F_{Ad} = \frac{1}{2} \rho C_d A_f (v - v_0)^2 \]  \hspace{1cm} (14)

4. EVALUATION OF THE ELECTRIC DIFFERENTIAL AND ITS CONSEQUENCES

Since the two rear wheels are directly driven by two independent motors, the speed of the outer wheel must differ from the speed of the inner wheel when cornering. This need can be easily satisfied if the position encoder can detect the angular position of the steering wheel. More details can be found in Figure 2. Figure 3. Presents the electric differential under the block diagram as applied for the numerical simulations based on the prior equation.

\[ \Delta w = w_{mes1} - w_{mes2} = -\frac{d_w \tan \delta}{L_w} w_v \]  \hspace{1cm} (15)

Next, the steering angle indicates the direction of the trajectory.

\[ \begin{align*}
\delta > 0 & \rightarrow \text{turn...left} \\
\delta < 0 & \rightarrow \text{turn...right} \\
\delta = 0 & \rightarrow \text{straight...ahead}
\end{align*} \hspace{1cm} (16)\]
5. CONTROL OF THE PMSM'S INPUT-OUTPUT LINEARIZATION

The input-output linearization technique converts the nonlinear system into a decoupled linear system by a nonlinear change in coordinates and feedback. The model of the engine in the $d$-$q$ frame of reference is provided [20]–[25], along with simplifying assumptions for the PMSM.

\[
\begin{align*}
\frac{di_d}{dt} &= -\frac{R_s}{L_d}i_d + \frac{L_q}{L_d}pw_r i_q + \frac{1}{L_d}u_d \\
\frac{di_q}{dt} &= -\frac{R_s}{L_q}i_q + \frac{L_d}{L_q}pw_r i_d - \frac{q_r}{L_q}pw_r + \frac{1}{L_q}u_q \\
\frac{dw_r}{dt} &= \frac{3p}{2l} (\varphi i_q + \lambda i_d i_q) - \frac{1}{J}T_L - \frac{B}{J}w_r 
\end{align*}
\]  

(17)

The $T_L$ is taken out of the equations in this model and will be treated as a disturbance. The dynamics of the system can then be rearranged as seen in (1), (5), and (17).

\[
x = f(x) + g_1(x).u_d + g_2(x).u_q
\]

(18)

Where,

\[
x = \begin{bmatrix} i_d \, w_r \end{bmatrix}^T
\]

\[
g_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}^T
\]

\[
g_2 = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}^T
\]

Next, comparing (17) and (18), we can obtain:

\[
f(x) = \begin{bmatrix} f_1 \\ f_2 \\ f_3 \end{bmatrix} = \begin{bmatrix} -\frac{R_s}{L_d}i_d + \frac{L_q}{L_d}pw_r i_q \\ -\frac{R_s}{L_q}i_q + \frac{L_d}{L_q}pw_r i_d - \frac{q_r}{L_q}pw_r \\ \frac{3p}{2l} (\varphi i_q + \lambda i_d i_q) - \frac{B}{J}w_r \end{bmatrix}
\]

(20)

If a direct relation must be established between the outputs $y$ and the inputs $u$ of the system, the output variable is chosen by $y_1 = i_d$ and $y_2 = w_r$. Consequently, the following could be a simple way to express the output dynamics:

\[
y_1 = i_d = h_1(x), \quad \forall h_1 = [1 \, 0 \, 0]
\]

(21)

\[
y_2 = w_r = h_2(x), \quad \forall h_2 = [0 \, 0 \, 1]
\]

(22)

The order of the system's relative degree can be used to determine if a nonlinear system admits input-output linearization under the condition of linearization. We determine the output relative degree in order to derive the nonlinear control law. The relative degree of the $d$-axis current $i_d = y_1$ [21].

\[
y_1 = L_i h_1(x) + L_g h_1(x)u_d + L_g h_1(x)u_q \\
= -\frac{R_s}{L_d}i_d + \frac{L_q}{L_d}pw_r i_q
\]

(23)

$r_i = 1$ is the relative degree of $y_1(x)$. The diagram of linearized system is presented in Figure 4 with more details.

The mechanical speed's proportional degree is $w_m = y_2$

\[
y_2 = L_i h_2(x) + L_g h_2(x)u_d + L_g h_1(x)u_q \\
= \frac{3p}{2l} (\varphi i_q + \lambda i_d i_q) - \frac{B}{J}w_r
\]

(24)

We note that the inputs $u$ doesn't be shown in (24), a second derivative became then necessary:
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\[ \dot{y}_2 = L_f h_2(x) + L_g f_2(x) u_d + L_g f_2(x) u_q \]

\[ = A\lambda f_1(x) + A(\psi + \lambda d) f_2(x) - \frac{B}{I} f_3(x) + \frac{A\lambda}{l_d} i_q u_d + \frac{A(\psi + \lambda d)}{l_q} u_q \]

where

\[ \Lambda = \frac{3p}{2j} \]

\[ \dot{y}_2(x) \] has a relative degree of \( r_2 = 2 \). The system's relative degree is equal to its order \( n \) (which is set to 3). It is a perfectly linear system. By using the (22) and (25):

\[ [\dot{y}_1 \dot{y}_2]^T = \xi(x) + D(x), u \]

where

\[ \xi = \left[ L_f h_2(x) L_f^2 h_2(x) \right]^T \]

\[ = \left[ \begin{array}{c}
\frac{B}{I} f_3(x) + \frac{B}{I} f_3(x) \\
A\lambda f_1(x) + A(\psi + \lambda d) f_2(x) - \frac{B}{I} f_3(x)
\end{array} \right] \]

and

\[ D(x) = \left[ \begin{array}{cc}
\frac{1}{l_d} & 0 \\
\frac{A\lambda}{l_d} & \frac{A(\psi + \lambda d)}{l_q}
\end{array} \right] \]

The output dynamics are of order two even though the system dynamics are of third order, indicating the presence of internal dynamics and the resulting stability, which could be easily verified. With the assumption of \( v_1 = \dot{y}_1 \) and \( v_2 = \ddot{y}_2 \) as new state variables in [22]–[27]. We use the following nonlinear state feedback to linearize the motor’s input-output behaviours in the closed loop.

\[ \left[ \begin{array}{c}
u_d \\
u_q\end{array} \right] = D^{-1}(x) \left[ \begin{array}{c} v_1 \\
v_2\end{array} \right] - \xi(x) \]

The decoupling matrix must \( D^{-1}(x) \) be invertible. When the linearizing law (30) is applied to the system (27), two mono-variable, linear, and decoupled sub-systems can be created.

\[ [\dot{y}_1 \dot{y}_2]^T = [v_1 v_2]^T \]

The internal inputs \( (v_1, v_2) \) are calculated (poles placement) by imposing static modes \( (i_{dref} and w_{ref}) \) and an error dynamic.

\[ \left\{ \begin{array}{c}
e_{id} + K_d e_1 = 0 \\
e_{w} + K_w e_w + K_{w1} e_w + K_{w2} e_w = 0
\end{array} \right\} \]

Figure 4. Block diagram of linearized system
6. RESULTS AND DESCRIPTION

Simulations were run utilizing the model of the drive wheel system to characterize the behavior as presented in Figure 5. They display motor current as well as each motor’s speed fluctuation. More details about simulation including discussion can be found in the following sections.

6.1. In the case of a straight road

During this time, the EV drives at a speed of 80 km/h. Figure 5, provides that the speed of an EV has two phases. In the first phase, a speed of 80 km/h, and between [0 3] sand between [3 5] s in the second phase with a speed equal to 60 km/h. The two back wheels are moving at the same speed, as can be seen. This indicates that in this instance, the electrical differential is inoperative. The following graph indicates that the main change experienced when utilizing $F_{pens} = 5.81$ between [2 3] s. The torque of the produced motor is audible. The electromagnetic motor torque is significantly improved by the slope effect on both the left and right sides of each motor. Figure 5 serves as an example of the system’s behavior.

![Figure 5. Straight road application](image)

6.2. A 60 km/h curved road is on the right

In this stage, we inform the user that the EV is driving at a speed of 80 km/h. Figure 6 describes the EV speed that has two phases. In the first phase, is located between [0 2] s at 80 km/h and [2 5] s at 60 Km/h. Once this speed is regular, the resistive torque given to the motor wheels as a whole cause the torque to revert to its initial value. Next, in [3.5 4.5] s means the speed changed during the curved road to stabilize the EV.

![Figure 6. Curved road](image)
7. CONCLUSION

In the propulsion model, there are two permanent magnet synchronous motors (PMSM). The direct component of the current is set to zero to increase the motor's output torque. Each driving wheel may be separately controlled at each curve according to the electronic differential, which is used in the calculations. The program Matlab/Simulink is used to implement modeling and simulation in order to evaluate the efficacy of the proposed solution. Simulation studies are conducted to verify the effectiveness of the suggested method. The outcomes show that this strategy is more accurate. In future work, a novel application will be provided using different recent techniques and real applications.

REFERENCES


BIOGRAPHIES OF AUTHORS

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